AQA

Please write clearly in block capitals.

Centre number | | | | | | Candidate number | | | | |

Surname _____

Forename(s) _____

Candidate signature _____

AS
FURTHER MATHEMATICS

Paper 2 – Statistics

Thursday 17 May 2018 Afternoon Time allowed: 1 hour 30 minutes

Materials
- You must have the AQA formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification. (You may use a graphical calculator.)
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Discrete **or** Mechanics). You will have 1 hour 30 minutes to complete **both** papers.

Instructions
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work you do not want to be marked.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	

Information
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 40.

Advice
- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

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Answer **all** questions in the spaces provided.

1 Let X be a continuous random variable with probability density function given by

$$f(x) = \begin{cases} \frac{3}{4}x(2-x) & 0 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

Find $P(X = 1)$

Circle your answer.

[1 mark]

0 $\quad \frac{1}{2} \quad \frac{3}{4} \quad \frac{27}{32}$

2 The discrete random variable Y has a Poisson distribution with mean 3

Find the value of $P(Y > 1)$ to three significant figures.

Circle your answer.

[1 mark]

0.149 0.199 0.801 0.950

3 The discrete random variable X has the following probability distribution

x	1	2	4	9
$P(X = x)$	0.2	0.4	0.35	0.05

The continuous random variable Y has the following probability density function

$$f(y) = \begin{cases} \frac{1}{64}y^3 & 0 \leq y \leq 4 \\ 0 & \text{otherwise} \end{cases}$$

Given that X and Y are independent, show that $E(X^2 + Y^2) = \frac{1327}{60}$

[4 marks]

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4 The waiting times for patients to see a doctor in a hospital can be modelled with a normal distribution with known variance of 10 minutes.

4 (a) A random sample of 100 patients has a total waiting time of 3540 minutes.

Calculate a 98% confidence interval for the population mean of waiting times, giving values to four significant figures.

[4 marks]

4 (b) Dante conducts a hypothesis test with the sample from part **(a)** on the waiting times. Dante's hypotheses are

$$H_0 : \mu = 38$$
$$H_1 : \mu \neq 38$$

Dante uses a 2% level of significance.

Explain whether Dante accepts or rejects the null hypothesis.

[1 mark]

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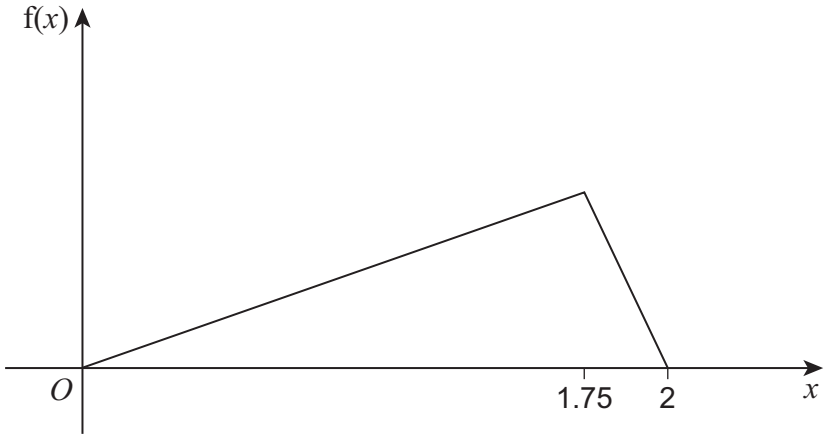
5 The diagram shows a graph of the probability density function of the random variable X.



5 (a) State the mode of X.

[1 mark]

5 (b) Find the probability density function of X.

[4 marks]

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6 The discrete random variable Y has the probability function

$$\mathrm{P}(Y = y) = \begin{cases} 2ky & y = 1, 2, 3, 4 \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

Show that $\mathrm{Var}(5Y - 2) = 25$

[6 marks]

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7 Over a period of time it has been shown that the mean number of vehicles passing a service station on a motorway is 50 per minute.

After a new motorway junction was built nearby, Xander observed that 30 vehicles passed the service station in one minute.

7 (a) Xander claims that the construction of the new motorway junction has reduced the mean number of vehicles passing the service station per minute.

Investigate Xander's claim, using a suitable test at the 1% level of significance.

[6 marks]

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7 (b) For your test carried out in part **(a)** state, in context, the meaning of a Type 1 error.

[1 mark]

_____

_____

_____

7 (c) Explain why the model used in part **(a)** might be invalid.

[1 mark]

_____

_____

_____

Turn over for the next question

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8 An insurance company groups its vehicle insurance policies into two categories, car insurance and motorbike insurance.

The number of claims in a random sample of 80 policies was monitored and the results summarised in contingency **Table 1**.

Table 1

		Number of claims				
		0	**1**	**2**	**3 or more**	**Total**
Type of insurance policy	**Car**	9	10	11	5	35
	Motorbike	19	13	8	5	45
	Total	28	23	19	10	80

The insurance company decides to carry out a χ^2-test for association between number of claims and type of insurance policy using the information given in **Table 1**.

8 (a) The contingency table shown in **Table 2** gives some of the exact expected frequencies for this test.

Complete **Table 2** with the missing exact expected values.

[2 marks]

Table 2

		Number of claims			
		0	**1**	**2**	**3 or more**
Type of insurance policy	**Car**		10.0625		4.375
	Motorbike			10.6875	

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8 (b) Carry out the insurance company's test, using the 10% level of significance.

[8 marks]

END OF QUESTIONS

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