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Centre number

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Candidate number

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Candidate signature

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I declare this is my own work.

# A-level

# FURTHER MATHEMATICS

## Paper 3 Statistics

Friday 7 June 2024

Afternoon

Time allowed: 2 hours

### Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a graphical or scientific calculator that meets the requirements of the specification.
- You must ensure you have the other optional Question Paper/Answer Book for which you are entered (**either** Discrete **or** Mechanics). You will have 2 hours to complete **both** papers.

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 50.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
<b>TOTAL</b>	



Answer **all** questions in the spaces provided.

- 1** The random variable  $X$  has a Poisson distribution with mean 16

Find the standard deviation of  $X$

Circle your answer.

**[1 mark]**

4

8

16

256

- 2** The random variable  $T$  has an exponential distribution with mean 2

Find  $P(T \leq 1.4)$

Circle your answer.

**[1 mark]**

$e^{-2.8}$

$e^{-0.7}$

$1 - e^{-0.7}$

$1 - e^{-2.8}$



- 3 The continuous random variable  $Y$  has **cumulative** distribution function

$$F(y) = \begin{cases} 0 & y < 2 \\ -\frac{1}{9}y^2 + \frac{10}{9}y - \frac{16}{9} & 2 \leq y < 5 \\ 1 & y \geq 5 \end{cases}$$

Find the median of  $Y$

Circle your answer.

[1 mark]

2

$\frac{10 - 3\sqrt{2}}{2}$

$\frac{7}{2}$

$\frac{10 + 3\sqrt{2}}{2}$

Turn over for the next question

Turn over ►



**[6 marks]**

[illegible]

**5**

$$f(x) = \begin{cases} \frac{1}{6} e^{\frac{x}{3}} & 0 \leq x \leq \ln 27 \\ 0 & \text{otherwise} \end{cases}$$

Show that the mean of  $X$  is  $\frac{3}{2}(\ln 27 - 2)$

**[5 marks]**

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**Turn over for the next question**

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The random variable  $Y$  has probability distribution function

$$P(Y=y) = \begin{cases} \frac{1}{n} & y = 13, 16, 19 \dots, 3n + 10 \\ 0 & \text{otherwise} \end{cases}$$

**7 (a)** State the variance of  $X$

**[1 mark]**

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**7 (b)** Hence find the variance of  $Y$

Fully justify your answer.

**[3 marks]**

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$x$	7	13	17	21
$P(X = x)$	0.4	0.35	0.1	0.15

Show that  $P(X \leq 17 \mid X > E(X)) = 0.75$

**[5 marks]**

[illegible]

**Turn over ►**



- 9** A company owns three shops, A, B and C, which are based in different towns.
- Each shop gives a questionnaire to 250 of their customers, and every customer completes the questionnaire.
- One of the questions asks whether the customer rates the shop as good, satisfactory or poor.
- For shop A, 26% of customers rate the shop as good and 38% of customers rate the shop as poor.
- For shop B, 32% of customers rate the shop as good and 40% of customers rate the shop as satisfactory.
- Altogether, there are 210 good ratings and 261 satisfactory ratings.

- 9 (a)** Complete the following table with the observed frequencies.

**[3 marks]**

		Rating		
		Good	Satisfactory	Poor
Shop	A			
	B			
	C			

- 9 (b)** Carry out a test for association between shop and rating, using the 1% level of significance.

**[8 marks]**

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[illegible]

**Turn over ►**



- 10** The length,  $X$  cm, of teeth for an extinct breed of shark is known to have a normal distribution.

A random sample of 250 teeth has the following summary statistics.

$\bar{x}$	$s$
10.2	1.3

- 10 (a)** Construct a 91% confidence interval for the population mean length of the shark teeth.

Give your limits to two decimal places.

**[3 marks]**

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- 10 (b)** The random sample is used to carry out a hypothesis test using the 9% level of significance.

The hypotheses are

$$H_0: \mu = 10.36$$

$$H_1: \mu \neq 10.36$$

- 10 (b) (i)** State, with a reason, whether the null hypothesis will be rejected.

**[1 mark]**

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- 10 (b) (ii)** The hypothesis test is repeated with a second random sample of 250 teeth which also has  $s = 1.3$  cm

Find the power of this test assuming that the population mean length of the shark teeth is 10.32 cm

Give your answer to two decimal places.

**[3 marks]**

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**END OF QUESTIONS**



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