

GCE

Further Mathematics B MEI

Y433/01: Modelling with algorithms

A Level

Mark Scheme for June 2024

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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MARKING INSTRUCTIONS

PREPARATION FOR MARKING RM ASSESSOR

1. Make sure that you have accessed and completed the relevant training packages for on-screen marking: *RM Assessor Online Training*; *OCR Essential Guide to Marking*.
2. Make sure that you have read and understood the mark scheme and the question paper for this unit. These are posted on the RM Cambridge Assessment Support Portal <http://www.rm.com/support/ca>
3. Log-in to RM Assessor and mark the **required number** of practice responses (“scripts”) and the **number of required** standardisation responses.

MARKING

1. Mark strictly to the mark scheme.
2. Marks awarded must relate directly to the marking criteria.
3. The schedule of dates is very important. It is essential that you meet the RM Assessor 50% and 100% (traditional 40% Batch 1 and 100% Batch 2) deadlines. If you experience problems, you must contact your Team Leader (Supervisor) without delay.

4. Annotations

| Annotation | Meaning |
|-------------------|-------------------------------|
| ✓ and ✖ | |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| E | Explanation mark 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| BP | Blank Page |
| Seen | |
| Highlighting | |

| Other abbreviations in mark scheme | Meaning |
|------------------------------------|---|
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By Calculator |
| DR | This question included the instruction: In this question you must show detailed reasoning. |

5. Subject Specific Marking Instructions

- a. Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

- b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

- c. The following types of marks are available.

M

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using

some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words “Determine” or “Show that”, or some other indication that the method must be given explicitly.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f. Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads "3 s.f".

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

- g. Rules for replaced work and multiple attempts:

- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- If a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

- h. For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors.

If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

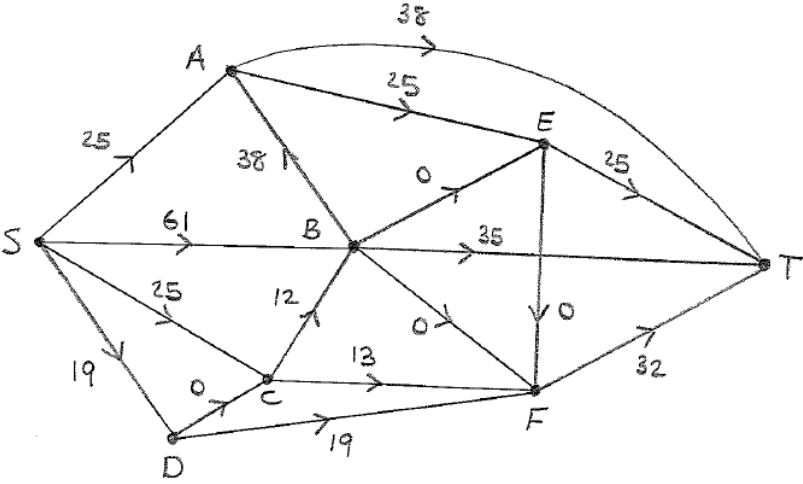
- i. If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” or “Determine”. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j. If in any case the scheme operates with considerable unfairness consult your Team Leader.

| Question | | | Answer | Marks | AO | Guidance |
|----------|-----|--|---|-----------|------------|--|
| 1 | (a) | | Container 1: 23 15 10 | M1 | 1.1 | First six numbers placed correctly (those in bold) |
| | | | Container 2: 17 18 12 | A1 | 1.1 | cao (no additional/repeated values) |
| | | | Container 3: 35 11 | | | |
| | | | Container 4: 21 22 | | | |
| | | | Container 5: 8 | [2] | | |
| 1 | (b) | | Container 1: 35 15 | M1 | 1.1 | First six numbers placed correctly (those in bold) |
| | | | Container 2: 23 22 | A1 | 1.1 | cao (no additional/repeated values) |
| | | | Container 3: 21 18 11 | | | |
| | | | Container 4: 17 12 10 8 | [2] | | |
| 1 | (c) | | e.g | B1 | 2.4 | Any valid reason for why the packing in part (b) is optimal e.g. two bins in part (b) are full and the remaining values total $100 > 92 > 50$ so 4 bins required |
| | | | Total = 192 and $192 \div 50 = 3.84$ so 4 containers is the lower bound hence the packing found in part (b) is optimal | [1] | | |

| Question | Answer | Marks | AO | Guidance |
|----------|--|---|---|--|
| 2 (a) | <div style="text-align: center;"> </div> <p>Shortest path from A to E: ACBHE</p> | <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>B1 [5]</p> | <p>1.2</p> <p>1.1a</p> <p>1.1a</p> <p>1.1</p> <p>1.1</p> | <p>Correct working values at B.</p> <p>Correct working values, condone a value of 54 after 49 at H, a value of 74 after 56 at F and a value of 68 after 59 at E. Condone no working value at A.</p> <p>Labels</p> <p>Order of labelling (starting from 0 or 1)</p> |

| Question | | | Answer | Marks | AO | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|-----|------|--|--------------------------------|-------------------------|---|----|----|---|---|---|---|--|---|---|---|---|---|---|---|---|---|--|----|----|--|--|--|--|--|---|----|--|---|----|--|--|----|----|---|----|---|--|----|--|----|----|----|---|--|----|----|--|----|--|--|--|---|--|--|--|----|--|----|----|----|---|--|--|----|--|----|--|--|----|---|--|----|----|--|----|--|--|----|---|--|----|----|--|----|----|----|--|---------------------------------------|----------------------------------|---|
| 2 | (b) | (i) | <table><tr><td></td><td>1</td><td>3</td><td>2</td><td>5</td><td>7</td><td>8</td><td>4</td><td>6</td></tr><tr><td></td><td>A</td><td>B</td><td>C</td><td>D</td><td>E</td><td>F</td><td>G</td><td>H</td></tr><tr><td>A</td><td></td><td>31</td><td>21</td><td></td><td></td><td></td><td></td><td></td></tr><tr><td>B</td><td>31</td><td></td><td>8</td><td>12</td><td></td><td></td><td>10</td><td>20</td></tr><tr><td>C</td><td>21</td><td>8</td><td></td><td>24</td><td></td><td>35</td><td>20</td><td>36</td></tr><tr><td>D</td><td></td><td>12</td><td>24</td><td></td><td>30</td><td></td><td></td><td></td></tr><tr><td>E</td><td></td><td></td><td></td><td>30</td><td></td><td>12</td><td>40</td><td>10</td></tr><tr><td>F</td><td></td><td></td><td>35</td><td></td><td>12</td><td></td><td></td><td>25</td></tr><tr><td>G</td><td></td><td>10</td><td>20</td><td></td><td>40</td><td></td><td></td><td>15</td></tr><tr><td>H</td><td></td><td>20</td><td>36</td><td></td><td>10</td><td>25</td><td>15</td><td></td></tr></table> <p>Total length: 88 (km)</p> | | 1 | 3 | 2 | 5 | 7 | 8 | 4 | 6 | | A | B | C | D | E | F | G | H | A | | 31 | 21 | | | | | | B | 31 | | 8 | 12 | | | 10 | 20 | C | 21 | 8 | | 24 | | 35 | 20 | 36 | D | | 12 | 24 | | 30 | | | | E | | | | 30 | | 12 | 40 | 10 | F | | | 35 | | 12 | | | 25 | G | | 10 | 20 | | 40 | | | 15 | H | | 20 | 36 | | 10 | 25 | 15 | | <p>M1</p> <p>A1</p> <p>B1 [3]</p> | <p>1.1</p> <p>1.1</p> <p>1.1</p> | <p>Choosing the 21 in column A, the 8 in column C, the 10 in column B and the 15 in column G (or 1, 3, 2, -, -, -, 4, -, - across the top of the table or A, C, B, G,... or AC, BC, BG,...)</p> <p>All circled values correct and all numbers correct across the top of the table</p> |
| | 1 | 3 | 2 | 5 | 7 | 8 | 4 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A | B | C | D | E | F | G | H | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | | 31 | 21 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | 31 | | 8 | 12 | | | 10 | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | 21 | 8 | | 24 | | 35 | 20 | 36 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | | 12 | 24 | | 30 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| E | | | | 30 | | 12 | 40 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| F | | | 35 | | 12 | | | 25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| G | | 10 | 20 | | 40 | | | 15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| H | | 20 | 36 | | 10 | 25 | 15 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | (b) | (ii) | | <p>B1</p> <p>[1]</p> | <p>1.1</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | (c) | | <p>88 – 12 = 76 (km)</p> | <p>B1FT</p> <p>[1]</p> | <p>3.1a</p> | <p>Their value from part (b)(i) – 12 (dependent on correct arcs in MST)</p> <p>Or total from their MST excluding their arc to D</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | (d) | | <p>$t = 0.016 \times \left(\frac{1000}{16}\right)^2$</p> <p>= 62.5 (s)</p> | <p>M1</p> <p>A1</p> <p>[2]</p> | <p>3.1b</p> <p>2.2b</p> | <p>Use of $n = 16$ and quadratic order – allow reciprocal or slip in the value 0.016 and 1000</p> <p>SCB1 $0.016 \times \left(\frac{1000}{n}\right)^2$ where $n = 7, 8$ or 32</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Question | Answer | Marks | AO | Guidance |
|----------|---|--|-------------------------------------|---|
| 3 (a) | | <p>B1</p> <p>B1</p> <p>[2]</p> | <p>3.3</p> <p>3.3</p> | <p>Correct arrows</p> <p>Correct values</p> <p>Ignore any cuts if shown on the diagram in this part.</p> |
| 3 (b) | Cut $\alpha = 38 + 25 + 40 + 49 + 17 + 26 + 19 = 214$ | <p>B1</p> <p>[1]</p> | 1.1 | |
| 3 (c) | $SA + SB + SC + SD = 25 + 61 + 37 + 35 = 158 < 214$ so the maximum flow cannot be equal to the value of the cut from part (b) (as the objective forms a cut and the maximum flow is equal to the minimum cut (so max. flow is at most 158)) | <p>B1FT</p> <p>[1]</p> | 2.2a | <p>Value 158 seen and correctly <u>compares</u> to their value in part (b) (provided value in part (b) is bigger)</p> <p>Allow $158 < \alpha$</p> |

| Question | | Answer | Marks | AO | Guidance |
|----------|--|---|--|--|---|
| 3 (d) | |  <p>Maximum flow through the network is 130 (litres/minute)</p> | <p>M1</p> <p>A1</p> <p>B1 [3]</p> | <p>3.4</p> <p>1.1</p> <p>2.2a</p> | <p>Consistent flow pattern (flow in = flow out at each node) – one number on each arc. SA = 25, SB = 61, AE = 25, AT = 38, BT = 35, CB = 12, DC = 0, DF = 19, EF = 0 and FT = 32</p> <p>Condone incorrect flow across one vertex for the M mark. Condone incorrect or missing arrows</p> <p>All values (including the zeros) and arrows correct on each arc</p> |
| 3 (e) | | <p>The cut which partitions the vertices into the sets {S, C, D, F}, {A, B, E, T} (with capacity 25 + 61 + 12 + 32 = 130)</p> <p>By the maximum flow-minimum cut theorem the maximum flow is equal to the minimum cut and so therefore the maximum flow through the system is 130 litres per minute (as indicated by the flow part (d))</p> | <p>M1</p> <p>A1</p> <p>[2]</p> | <p>3.1b</p> <p>2.1</p> | <p>Allow listing of cut arcs (SA, SB, CB, BF, EF, FT) - allow cut shown on diagram only if explicitly referred to here.</p> <p>Requires correct cut, 130 stated and mention of max flow-min cut theorem (o.e.)</p> |
| 3 (f) | | <p>Change the constraint $CB \leq 12$ to $BC \leq 12$</p> <p>Change the constraints:</p> $SB + CB - BA - BE - BF - BT = 0 \text{ to}$ $SB - BC - BA - BE - BF - BT = 0$ <p>and</p> $SC + DC - CB - CF = 0 \text{ to } SC + DC + BC - CF = 0$ <p>(no other changes required)</p> | <p>B1</p> <p>B1</p> <p>[2]</p> | <p>3.5c</p> <p>2.5</p> | <p>Change must be stated or explained.</p> |

| Question | | | Answer | Marks | AO | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|------------|------------|--|-----------|-------------|--|-------|-------|-------|-------|-------|-------|-------|-----|---|---|---|---|---|---|---|---|----|---|-----|---|---|---|---|----|---|---|---|---|---|---|---|---|----|---|---|---|---|---|---|---|----|---|---|---|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|-----|---|---|---|---|---|---|---|---|----|---|-----|
| 4 | | | $x + y + z = 180$ | B1 | 3.1a | Possibly implied by later working | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $x \geq z - 10$ or $-x + z + s_1 = 10$ | M1 | 3.3 | Allow $x \leq z - 10$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $y \geq 2z$ or $-y + 2z + s_2 = 0$ | M1 | 3.3 | Allow $y \leq 2z$ or $2y \geq z$ or $2y \leq z$ for this mark | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $P - z = 0$ | A1 | 1.1 | At least two correct equations | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $-x + z + s_1 = 10$ | A1 | 1.1 | All correct equations possibly implied by later working (e.g. values in tableau). | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $-y + 2z + s_2 = 0$ | | | Allow any equivalent (correct) forms for both marks. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $x + y + z + s_3 = 180$ | | | If A0A0 then B1 for at least 2 correct equations. | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $x + y + z - s_4 + a_4 = 180$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | $A = a_4 = 180 - x - y - z + s_4$ ($\Rightarrow A + x + y + z - s_4 = 180$) | M1 | 2.1 | Forming second objective with only one artificial variable and in terms of x, y, z and one surplus variable only | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | <table><tr><th>A</th><th>P</th><th>x</th><th>y</th><th>z</th><th>s_1</th><th>s_2</th><th>s_3</th><th>s_4</th><th>a_4</th><th>RHS</th></tr><tr><td>1</td><td>0</td><td>1</td><td>1</td><td>1</td><td>0</td><td>0</td><td>0</td><td>-1</td><td>0</td><td>180</td></tr><tr><td>0</td><td>1</td><td>0</td><td>0</td><td>-1</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>0</td><td>-1</td><td>0</td><td>1</td><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td><td>10</td></tr><tr><td>0</td><td>0</td><td>0</td><td>-1</td><td>2</td><td>0</td><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td>0</td><td>0</td><td>1</td><td>0</td><td>0</td><td>180</td></tr><tr><td>0</td><td>0</td><td>1</td><td>1</td><td>1</td><td>0</td><td>0</td><td>0</td><td>-1</td><td>1</td><td>180</td></tr></table> | A | P | x | y | z | s_1 | s_2 | s_3 | s_4 | a_4 | RHS | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | -1 | 0 | 180 | 0 | 1 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | -1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 10 | 0 | 0 | 0 | -1 | 2 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 180 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | -1 | 1 | 180 |
| A | P | x | y | z | s_1 | s_2 | s_3 | s_4 | a_4 | RHS | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | -1 | 0 | 180 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 1 | 0 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | -1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 0 | -1 | 2 | 0 | 1 | 0 | 0 | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 180 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | -1 | 1 | 180 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A1 | 1.1 | cao | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | [8] | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Question | | | Answer | Marks | AO | Guidance |
|----------|-----|------|---|---|---|---|
| 5 | (a) | | | M1 A1 A1 [3] | 3.3 1.1 3.1a | Activity on arc, one start + IPAs for A, B, C, D, E and F correct (so starting from the correct event). Allow missing arrows for this mark. IPAs for activities G, H, I, J and K correct (so starting from the correct event). Allow missing arrows for this mark. One finish, correct dummies + all arrows correct |
| 5 | (b) | (i) | Critical activities: A, E, F and H | B1 [1] | 3.4 | cao – no additional activities |
| 5 | (b) | (ii) | Minimum project completion time is 19 (hours) | B1 [1] | 1.1 | |

| Question | | | Answer | Marks | AO | Guidance | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|------|-----------------------------------|--|-------------|-------------|--------------------------------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|------|-----|---|
| 5 | (c) | | <table><tr><th>Activity</th><th>Total Float</th></tr><tr><td>A</td><td>0</td></tr><tr><td>B</td><td>5</td></tr><tr><td>C</td><td>6</td></tr><tr><td>D</td><td>6</td></tr><tr><td>E</td><td>0</td></tr><tr><td>F</td><td>0</td></tr><tr><td>G</td><td>4</td></tr><tr><td>H</td><td>0</td></tr><tr><td>I</td><td>2</td></tr><tr><td>J</td><td>8</td></tr><tr><td>K</td><td>7</td></tr></table> | Activity | Total Float | A | 0 | B | 5 | C | 6 | D | 6 | E | 0 | F | 0 | G | 4 | H | 0 | I | 2 | J | 8 | K | 7 | B1FT | 1.1 | Zero (total) float for their critical activities from part (b)(i) |
| | | | Activity | Total Float | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | A | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | B | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | C | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | D | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | E | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | F | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | G | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | H | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | I | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | J | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | K | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B1 | 3.1b | Two correct non-zero floats | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B1 | 1.1 | Four correct non-zero floats | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B1 | 1.1 | All seven correct non-zero floats | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| [4] | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | (d) | (i) | New min. projection completion time = 20 (hours) | B1 [1] | 3.1b | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | (d) | (ii) | New critical activities are A, E, G, L | B1 [1] | 2.2a | cao – no additional activities | | | | | | | | | | | | | | | | | | | | | | | | |

| Question | | | Answer | Marks | AO | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|-----|------|---|-----------------------------------|---------------------------------|--|----------------|-------|-------|-------|-----|---|---|---|------|---|---|---|----|---|---|---|----------------|---|----------------|----------------|----------------|---|---|---|------|---|---------------|---------------|----|---|---|---|----------------|---|---|---------------|----------------|-------------------------------|---------------------------|--|
| 6 | (a) | | 20 | B1 [1] | 1.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (b) | | The variable y is now a basic variable (rather than a non-basic variable) as indicated by three zeros and a single 1 in that column | B1 [1] | 2.4 | Correct reasoning – must mention either that <u>y is a basic variable</u> or <u>all zeros and a single 1 in that column</u> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (c) | | Maximise $P = 2x + 3y - z$ Subject to $x + y + 3z \leq 50$ $2x - 3y \leq 20$ $3y - 2z \leq 20$ $x, y, z \geq 0$ | B1 B1 B1 B1 B1 [5] | 3.4 2.1 1.1 1.1 1.1 | (See additional guidance) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (d) | | <table border="1"><thead><tr><th>P</th><th>x</th><th>y</th><th>z</th><th>s_1</th><th>s_2</th><th>s_3</th><th>RHS</th></tr></thead><tbody><tr><td>1</td><td>0</td><td>0</td><td>-3</td><td>0</td><td>1</td><td>2</td><td>60</td></tr><tr><td>0</td><td>0</td><td>0</td><td>$\frac{14}{3}$</td><td>1</td><td>$-\frac{1}{2}$</td><td>$-\frac{5}{6}$</td><td>$\frac{70}{3}$</td></tr><tr><td>0</td><td>1</td><td>0</td><td>-1</td><td>0</td><td>$\frac{1}{2}$</td><td>$\frac{1}{2}$</td><td>20</td></tr><tr><td>0</td><td>0</td><td>1</td><td>$-\frac{2}{3}$</td><td>0</td><td>0</td><td>$\frac{1}{3}$</td><td>$\frac{20}{3}$</td></tr></tbody></table> | P | x | y | z | s_1 | s_2 | s_3 | RHS | 1 | 0 | 0 | -3 | 0 | 1 | 2 | 60 | 0 | 0 | 0 | $\frac{14}{3}$ | 1 | $-\frac{1}{2}$ | $-\frac{5}{6}$ | $\frac{70}{3}$ | 0 | 1 | 0 | -1 | 0 | $\frac{1}{2}$ | $\frac{1}{2}$ | 20 | 0 | 0 | 1 | $-\frac{2}{3}$ | 0 | 0 | $\frac{1}{3}$ | $\frac{20}{3}$ | M1 A1 A1 [3] | 3.4 1.1 1.1 | Pivot (third) row and column (x) correct One of columns z, s_2, s_3 or RHS correct cao |
| P | x | y | z | s_1 | s_2 | s_3 | RHS | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0 | 0 | -3 | 0 | 1 | 2 | 60 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 0 | $\frac{14}{3}$ | 1 | $-\frac{1}{2}$ | $-\frac{5}{6}$ | $\frac{70}{3}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 1 | 0 | -1 | 0 | $\frac{1}{2}$ | $\frac{1}{2}$ | 20 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 1 | $-\frac{2}{3}$ | 0 | 0 | $\frac{1}{3}$ | $\frac{20}{3}$ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (e) | (i) | $x = 25, y = 10, z = 5$ | B1 [1] | 1.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (e) | (ii) | Substitute into either $P - 2x - z = 20$ or $P - 3z = 60$ or $P = 2x + 3y - z$ 75 | M1FT A1 [2] | 3.1b 1.1 | Substituting their values of x, y , and z from part (e)(i) into either of the three equations containing P | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Question 6c Additional guidance:

Method 1:

Find original $R1$

$$\text{old } R1 + A \times R4 = \text{new } R1$$

$$0 + A \times \frac{20}{3} = 20$$

$$A = 3$$

$$\therefore \text{old } R1 = \text{new } R1 - 3R4$$

Find original $R2$

$$\text{old } R2 + B \times R4 = \text{new } R2$$

$$0 + B \times \frac{1}{3} = -\frac{1}{3}$$

$$B = -1$$

$$\therefore \text{old } R2 = \text{new } R2 + R4$$

Find original $R3$

$$\text{old } R3 + C \times R4 = \text{new } R3$$

$$0 + C \times \frac{1}{3} = 1$$

$$C = 3$$

$$\therefore \text{old } R3 = \text{new } R3 - 3R4$$

| | P | x | y | z | s_1 | s_2 | s_3 | RHS |
|-----------------|-----|-----|-----|-----|-------|-------|-------|-------|
| <i>old</i> $R1$ | 1 | -2 | -3 | 1 | 0 | 0 | 0 | 0 |
| <i>old</i> $R2$ | 0 | 1 | 1 | 3 | 1 | 0 | 0 | 50 |
| <i>old</i> $R3$ | 0 | 2 | -3 | 0 | 0 | 1 | 0 | 20 |
| <i>old</i> $R4$ | 0 | 0 | 3 | -2 | 0 | 0 | 1 | 20 |

Method 2:

$$P = 20 - 3y + 2z$$

$$\Rightarrow P - 2x - z + 20 - 3y + 2z = 20$$

$$\Rightarrow P - 2x - 3y + z = 0$$

$$x + \frac{11}{3}z + s_1 + y - \frac{2}{3}z - \frac{20}{3} = \frac{130}{3}$$

$$x + y + 3z + s_1 = 50$$

$$\Rightarrow x + y + 3z \leq 50$$

$$2x - 2z + s_2 + 20 - 3y + 2z = 40$$

$$2x - 3y + s_2 = 20$$

$$\Rightarrow 2x - 3y \leq 20$$

$$y - \frac{2}{3}z + \frac{1}{3}s_3 = \frac{20}{3}$$

$$\Rightarrow 3y - 2z \leq 20$$

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