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2. Find

$$\int (12x^5 - 3x^2 + 4x^{\frac{1}{3}}) dx$$

giving each term in its simplest form.

(5)

Ruled area for the student's answer.

(Total 5 marks)

Q2





4. A sequence  $a_1, a_2, a_3, \dots$  is defined by

$$a_1 = 2$$
$$a_{n+1} = 3a_n - c$$

where  $c$  is a constant.

(a) Find an expression for  $a_2$  in terms of  $c$ . (1)

Given that  $\sum_{i=1}^3 a_i = 0$

(b) find the value of  $c$ . (4)

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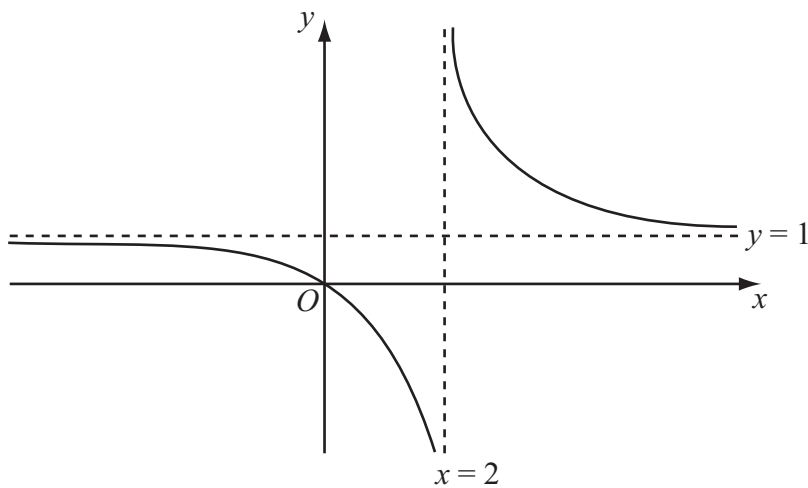
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5.



**Figure 1**

Figure 1 shows a sketch of the curve with equation  $y = f(x)$  where

$$f(x) = \frac{x}{x-2}, \quad x \neq 2$$

The curve passes through the origin and has two asymptotes, with equations  $y = 1$  and  $x = 2$ , as shown in Figure 1.

- (a) In the space below, sketch the curve with equation  $y = f(x-1)$  and state the equations of the asymptotes of this curve. **(3)**
  
- (b) Find the coordinates of the points where the curve with equation  $y = f(x-1)$  crosses the coordinate axes. **(4)**













9. The line  $L_1$  has equation  $2y - 3x - k = 0$ , where  $k$  is a constant.

Given that the point  $A(1, 4)$  lies on  $L_1$ , find

(a) the value of  $k$ , (1)

(b) the gradient of  $L_1$ . (2)

The line  $L_2$  passes through  $A$  and is perpendicular to  $L_1$ .

(c) Find an equation of  $L_2$  giving your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. (4)

The line  $L_2$  crosses the  $x$ -axis at the point  $B$ .

(d) Find the coordinates of  $B$ . (2)

(e) Find the exact length of  $AB$ . (2)

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10. (a) On the axes below, sketch the graphs of

(i)  $y = x(x+2)(3-x)$

(ii)  $y = -\frac{2}{x}$

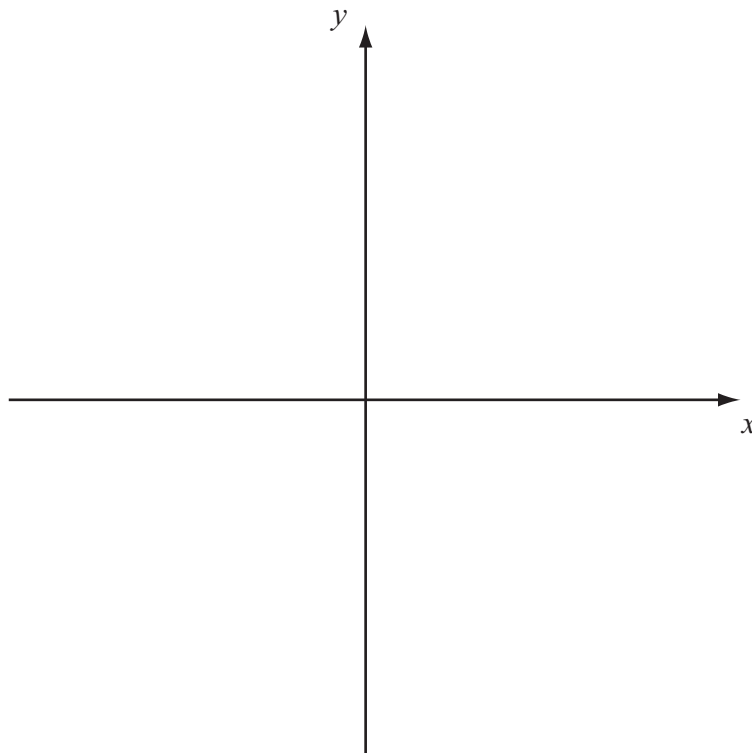
showing clearly the coordinates of all the points where the curves cross the coordinate axes.

(6)

(b) Using your sketch state, giving a reason, the number of real solutions to the equation

$$x(x+2)(3-x) + \frac{2}{x} = 0$$

(2)



11. The curve  $C$  has equation

$$y = \frac{1}{2}x^3 - 9x^{\frac{3}{2}} + \frac{8}{x} + 30, \quad x > 0$$

- (a) Find  $\frac{dy}{dx}$ . (4)
- (b) Show that the point  $P(4, -8)$  lies on  $C$ . (2)
- (c) Find an equation of the normal to  $C$  at the point  $P$ , giving your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers. (6)

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