

3.

$$x^2 - 8x - 29 \equiv (x + a)^2 + b,$$

where a and b are constants.

(a) Find the value of a and the value of b .

(3)

(b) Hence, or otherwise, show that the roots of

$$x^2 - 8x - 29 = 0$$

are $c \pm d\sqrt{5}$, where c and d are integers to be found.

(3)



4.

Figure 1

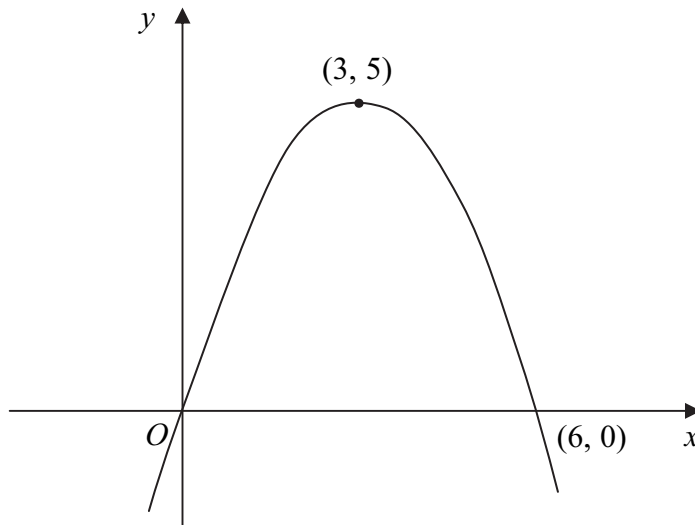


Figure 1 shows a sketch of the curve with equation $y = f(x)$. The curve passes through the origin O and through the point $(6, 0)$. The maximum point on the curve is $(3, 5)$.

On separate diagrams, sketch the curve with equation

(a) $y = 3f(x)$, (2)

(b) $y = f(x + 2)$. (3)

On each diagram, show clearly the coordinates of the maximum point and of each point at which the curve crosses the x -axis.



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7. (a) Show that $\frac{(3-\sqrt{x})^2}{\sqrt{x}}$ can be written as $9x^{-\frac{1}{2}} - 6 + x^{\frac{1}{2}}$. (2)

Given that $\frac{dy}{dx} = \frac{(3-\sqrt{x})^2}{\sqrt{x}}$, $x > 0$, and that $y = \frac{2}{3}$ at $x = 1$,

(b) find y in terms of x . (6)



8. The line l_1 passes through the point $(9, -4)$ and has gradient $\frac{1}{3}$.

(a) Find an equation for l_1 in the form $ax + by + c = 0$, where a , b and c are integers. (3)

The line l_2 passes through the origin O and has gradient -2 . The lines l_1 and l_2 intersect at the point P .

(b) Calculate the coordinates of P . (4)

Given that l_1 crosses the y -axis at the point C ,

(c) calculate the exact area of $\triangle OCP$. (3)



9. An arithmetic series has first term a and common difference d .

(a) Prove that the sum of the first n terms of the series is

$$\frac{1}{2}n[2a + (n-1)d]. \tag{4}$$

Sean repays a loan over a period of n months. His monthly repayments form an arithmetic sequence.

He repays £149 in the first month, £147 in the second month, £145 in the third month, and so on. He makes his final repayment in the n th month, where $n > 21$.

(b) Find the amount Sean repays in the 21st month. (2)

Over the n months, he repays a total of £5000.

(c) Form an equation in n , and show that your equation may be written as

$$n^2 - 150n + 5000 = 0. \tag{3}$$

(d) Solve the equation in part (c). (3)

(e) State, with a reason, which of the solutions to the equation in part (c) is **not** a sensible solution to the repayment problem. (1)



10. The curve C has equation $y = \frac{1}{3}x^3 - 4x^2 + 8x + 3$.

The point P has coordinates $(3, 0)$.

(a) Show that P lies on C . **(1)**

(b) Find the equation of the tangent to C at P , giving your answer in the form $y = mx + c$, where m and c are constants. **(5)**

Another point Q also lies on C . The tangent to C at Q is parallel to the tangent to C at P .

(c) Find the coordinates of Q . **(5)**



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Question 10 continued

Lined area for writing the answer to Question 10.

Q10

(Total 11 marks)

TOTAL FOR PAPER: 75 MARKS

END

