





2. Find

$$\int \left( 10x^4 - 4x - \frac{3}{\sqrt{x}} \right) dx$$

giving each term in its simplest form.

(4)

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Q2

(Total 4 marks)





4. A sequence  $a_1, a_2, a_3, \dots$  is defined by

$$\begin{aligned} a_1 &= 4 \\ a_{n+1} &= k(a_n + 2), \quad \text{for } n \geq 1 \end{aligned}$$

where  $k$  is a constant.

- (a) Find an expression for  $a_2$  in terms of  $k$ .

**(1)**

Given that  $\sum_{i=1}^3 a_i = 2$ ,

- (b) find the two possible values of  $k$ .

**(6)**



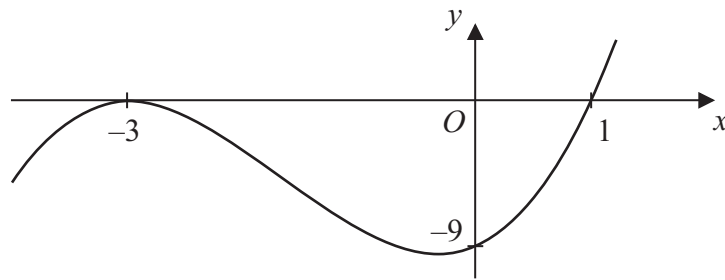








8.



**Figure 1**

Figure 1 shows a sketch of the curve with equation  $y = f(x)$  where

$$f(x) = (x + 3)^2 (x - 1), \quad x \in \mathbb{R}.$$

The curve crosses the  $x$ -axis at  $(1, 0)$ , touches it at  $(-3, 0)$  and crosses the  $y$ -axis at  $(0, -9)$

- (a) In the space below, sketch the curve  $C$  with equation  $y = f(x + 2)$  and state the coordinates of the points where the curve  $C$  meets the  $x$ -axis. **(3)**
  
- (b) Write down an equation of the curve  $C$ . **(1)**
  
- (c) Use your answer to part (b) to find the coordinates of the point where the curve  $C$  meets the  $y$ -axis. **(2)**





9.

$$f'(x) = \frac{(3 - x^2)^2}{x^2}, \quad x \neq 0$$

(a) Show that  $f'(x) = 9x^{-2} + A + Bx^2$ ,

where  $A$  and  $B$  are constants to be found.

(3)

(b) Find  $f''(x)$ .

(2)

Given that the point  $(-3, 10)$  lies on the curve with equation  $y = f(x)$ ,

(c) find  $f(x)$ .

(5)

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10. Given the simultaneous equations

$$\begin{aligned}2x + y &= 1 \\x^2 - 4ky + 5k &= 0\end{aligned}$$

where  $k$  is a non zero constant,

(a) show that

$$x^2 + 8kx + k = 0 \tag{2}$$

Given that  $x^2 + 8kx + k = 0$  has equal roots,

(b) find the value of  $k$ . (3)

(c) For this value of  $k$ , find the solution of the simultaneous equations. (3)

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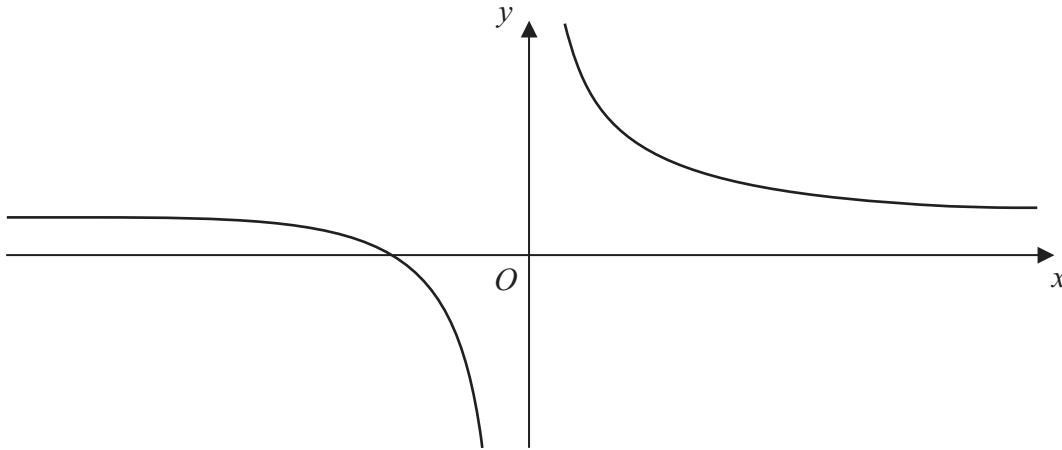
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11.



**Figure 2**

Figure 2 shows a sketch of the curve  $H$  with equation  $y = \frac{3}{x} + 4$ ,  $x \neq 0$ .

(a) Give the coordinates of the point where  $H$  crosses the  $x$ -axis. (1)

(b) Give the equations of the asymptotes to  $H$ . (2)

(c) Find an equation for the normal to  $H$  at the point  $P(-3, 3)$ . (5)

This normal crosses the  $x$ -axis at  $A$  and the  $y$ -axis at  $B$ .

(d) Find the length of the line segment  $AB$ . Give your answer as a surd. (3)

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