



1. A railway truck  $P$ , of mass  $m$  kg, is moving along a straight horizontal track with speed  $15 \text{ m s}^{-1}$ . Truck  $P$  collides with a truck  $Q$  of mass 3000 kg, which is at rest on the same track. Immediately after the collision the speed of  $P$  is  $3 \text{ m s}^{-1}$  and the speed of  $Q$  is  $9 \text{ m s}^{-1}$ . The direction of motion of  $P$  is reversed by the collision.

Modelling the trucks as particles, find

- (a) the magnitude of the impulse exerted by  $P$  on  $Q$ , (2)

- (b) the value of  $m$ . (3)

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2. A car of mass 1000 kg is towing a caravan of mass 750 kg along a straight horizontal road. The caravan is connected to the car by a tow-bar which is parallel to the direction of motion of the car and the caravan. The tow-bar is modelled as a light rod. The engine of the car provides a constant driving force of 3200 N. The resistances to the motion of the car and the caravan are modelled as constant forces of magnitude 800 newtons and  $R$  newtons respectively.

Given that the acceleration of the car and the caravan is  $0.88 \text{ ms}^{-2}$ ,

- (a) show that  $R=860$ , (3)

- (b) find the tension in the tow-bar. (3)

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3. Three forces  $\mathbf{F}_1$ ,  $\mathbf{F}_2$  and  $\mathbf{F}_3$  acting on a particle  $P$  are given by

$$\mathbf{F}_1 = (7\mathbf{i} - 9\mathbf{j}) \text{ N}$$

$$\mathbf{F}_2 = (5\mathbf{i} + 6\mathbf{j}) \text{ N}$$

$$\mathbf{F}_3 = (p\mathbf{i} + q\mathbf{j}) \text{ N}$$

where  $p$  and  $q$  are constants.

Given that  $P$  is in equilibrium,

- (a) find the value of  $p$  and the value of  $q$ . (3)

The force  $\mathbf{F}_3$  is now removed. The resultant of  $\mathbf{F}_1$  and  $\mathbf{F}_2$  is  $\mathbf{R}$ .  
Find

- (b) the magnitude of  $\mathbf{R}$ , (2)

- (c) the angle, to the nearest degree, that the direction of  $\mathbf{R}$  makes with  $\mathbf{j}$ . (3)

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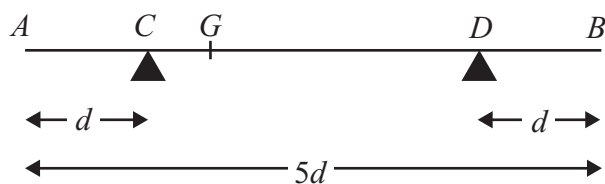
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**Figure 1**

A non-uniform rod  $AB$ , of mass  $m$  and length  $5d$ , rests horizontally in equilibrium on two supports at  $C$  and  $D$ , where  $AC = DB = d$ , as shown in Figure 1. The centre of mass of the rod is at the point  $G$ . A particle of mass  $\frac{5}{2}m$  is placed on the rod at  $B$  and the rod is on the point of tipping about  $D$ .

(a) Show that  $GD = \frac{5}{2}d$ . (4)

The particle is moved from  $B$  to the mid-point of the rod and the rod remains in equilibrium.

(b) Find the magnitude of the normal reaction between the support at  $D$  and the rod. (5)

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6. A car moves along a straight horizontal road from a point  $A$  to a point  $B$ , where  $AB=885$  m. The car accelerates from rest at  $A$  to a speed of  $15\text{ m s}^{-1}$  at a constant rate  $a\text{ m s}^{-2}$ . The time for which the car accelerates is  $\frac{1}{3}T$  seconds. The car maintains the speed of  $15\text{ m s}^{-1}$  for  $T$  seconds. The car then decelerates at a constant rate of  $2.5\text{ m s}^{-2}$  stopping at  $B$ .
- (a) Find the time for which the car decelerates. (2)
- (b) Sketch a speed-time graph for the motion of the car. (2)
- (c) Find the value of  $T$ . (4)
- (d) Find the value of  $a$ . (2)
- (e) Sketch an acceleration-time graph for the motion of the car. (3)

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7. [In this question, the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are due east and due north respectively. Position vectors are relative to a fixed origin  $O$ .]

A boat  $P$  is moving with constant velocity  $(-4\mathbf{i} + 8\mathbf{j}) \text{ km h}^{-1}$ .

(a) Calculate the speed of  $P$ . (2)

When  $t = 0$ , the boat  $P$  has position vector  $(2\mathbf{i} - 8\mathbf{j}) \text{ km}$ . At time  $t$  hours, the position vector of  $P$  is  $\mathbf{p} \text{ km}$ .

(b) Write down  $\mathbf{p}$  in terms of  $t$ . (1)

A second boat  $Q$  is also moving with constant velocity. At time  $t$  hours, the position vector of  $Q$  is  $\mathbf{q} \text{ km}$ , where

$$\mathbf{q} = 18\mathbf{i} + 12\mathbf{j} - t(6\mathbf{i} + 8\mathbf{j})$$

Find

(c) the value of  $t$  when  $P$  is due west of  $Q$ , (3)

(d) the distance between  $P$  and  $Q$  when  $P$  is due west of  $Q$ . (3)

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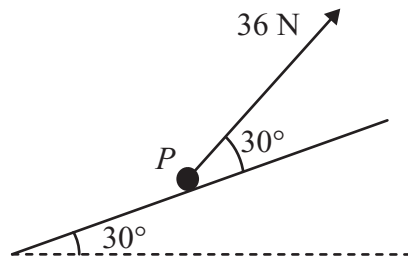


Figure 2

A particle  $P$  of mass  $4\text{ kg}$  is moving up a fixed rough plane at a constant speed of  $16\text{ m s}^{-1}$  under the action of a force of magnitude  $36\text{ N}$ . The plane is inclined at  $30^\circ$  to the horizontal. The force acts in the vertical plane containing the line of greatest slope of the plane through  $P$ , and acts at  $30^\circ$  to the inclined plane, as shown in Figure 2. The coefficient of friction between  $P$  and the plane is  $\mu$ . Find

- (a) the magnitude of the normal reaction between  $P$  and the plane, (4)
- (b) the value of  $\mu$ . (5)

The force of magnitude  $36\text{ N}$  is removed.

- (c) Find the distance that  $P$  travels between the instant when the force is removed and the instant when it comes to rest. (5)

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