

Mark Scheme (Results)

January 2007

GCE

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Statistics S2 (6684)

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Question Number	Scheme	Marks
1. (a)	A random variable; function of known observations (from a population). data OK	B1 B1 (2)
(b) (i)	Yes	B1
(ii)	No	B1 (1)
		Total 4
2. (a)	$P(J \geq 10) = 1 - P(J \leq 9)$ $= 1 - 0.9919$ $= 0.0081$	M1 A1 (2)
	or $= 1 - P(J < 10)$ implies method awrt 0.0081	
(b)	$P(K \leq 1) = P(K = 0) + P(K = 1)$ both, implied below even with '25' missing $= (0.73)^{25} + 25(0.73)^{24}(0.27)$ $= 0.00392$	M1 M1 A1 (3)
	clear attempt at '25' required awrt 0.0039 implies M	Total 5

Question Number	Scheme	Marks	
3. (a)	<p>Let W represent the number of white plants.</p> $W \sim B(12, 0.45)$ $P(W=5) = P(W \leq 5) - P(W \leq 4)$ $= 0.5269 - 0.3044$ $= 0.2225$	<p style="text-align: right;">use of ${}^{12}C_5 0.45^5 0.55^7$ or equivalent award B1M1</p> <p style="text-align: right;">values from correct table implies B</p> <p style="text-align: right;">awrt 0.222(5)</p>	B1 M1
(b)	$P(W \geq 7) = 1 - P(W \leq 6)$ $= 1 - 0.7393$ $= 0.2607$	<p style="text-align: right;">or $= 1 - P(W < 7)$</p> <p style="text-align: right;">implies method</p> <p style="text-align: right;">awrt 0.261</p>	M1
(c)	$P(\text{3 contain more white than coloured}) = \frac{10!}{3!7!} (0.2607)^3 (1 - 0.2607)^7$ $= 0.256654\dots$	<p style="text-align: right;">use of B,n=10</p> <p style="text-align: right;">awrt 0.257</p>	M1A1
(d)	<p>mean = $np = 22.5$; var = $npq = 12.375$</p> $P(W > 25) \approx P\left(Z > \frac{25.5 - 22.5}{\sqrt{12.375}}\right)$ $\approx P(Z > 0.8528\dots)$ $\approx 1 - 0.8023$ ≈ 0.1977	<p style="text-align: right;">\pm standardise with σ and μ; ± 0.5 c.c.</p> <p style="text-align: right;">awrt 0.85</p> <p style="text-align: right;">‘one minus’</p> <p style="text-align: right;">awrt 0.197 or 0.198</p>	B1B1 M1;M1
		(7)	
		Total 15	

Question Number	Scheme	Marks
4. (a)	$\lambda > 10$ or large μ ok	B1 (1)
(b)	The Poisson is discrete and the normal is continuous.	B1 (1)
(c)	Let Y represent the number of yachts hired in winter $P(Y < 3) = P(Y \leq 2)$ $= 0.1247$ awrt 0.125	$P(Y \leq 2) \& \text{Po}(5)$ M1 A1 (2)
(d)	Let X represent the number of yachts hired in summer $X \sim \text{Po}(25)$. $N(25, 25)$ all correct, can be implied by standardisation below $P(X > 30) \approx P\left(Z > \frac{30.5 - 25}{5}\right)$ ± standardise with 25 & 5; ±0.5 c.c. $\approx P(Z > 1.1)$ $\approx 1 - 0.8643$ ≈ 0.1357 awrt 0.136	B1 M1;M1 A1 M1 A1 (6)
(e)	no. of weeks = 0.1357×16 $= 2.17$ or 2 or 3	ANS (d)x16 ans>16 M0A0 A1 (2) Total 12

Question Number	Scheme	Marks
5.		
(a)	$f(x) = \begin{cases} \frac{1}{\beta - \alpha}, & \alpha < x < \beta, \\ 0, & \text{otherwise.} \end{cases}$ function including inequality, 0 otherwise	B1,B1 (2)
(b)	$\frac{\alpha + \beta}{2} = 2, \quad \frac{3 - \alpha}{\beta - \alpha} = \frac{5}{8}$ $\alpha + \beta = 4$ $3\alpha + 5\beta = 24$	B1,B1
	$3(4 - \beta) + 5\beta = 24$ $2\beta = 12$ $\beta = 6$	attempt to solve 2 eqns M1
	$\alpha = -2$	both A1 (4)
(c)	$E(X) = \frac{150 + 0}{2} = 75 \text{ cm}$	75 B1 (1)
(d)	Standard deviation = $\sqrt{\frac{1}{12}(150 - 0)^2}$ $= 43.30127\dots \text{cm}$	M1 $25\sqrt{3}$ or awrt 43.3 A1 (2)
(e)	$P(X < 30) + P(X > 120) = \frac{30}{150} + \frac{30}{150}$ 1st or at least one fraction, + or double $= \frac{60}{150}$ or $\frac{2}{5}$ or 0.4 or equivalent fraction	M1,M1 A1 (3)
		Total 12

Question Number	Scheme	Marks
6. (a)	$H_0 : p = 0.20, H_1 : p < 0.20$ Let X represent the number of people buying family size bar. $X \sim B(30, 0.20)$ $P(X \leq 2) = 0.0442$ or $P(X \leq 2) = 0.0442$ awrt 0.044 $P(X \leq 3) = 0.1227$ $CR X \leq 2$ $0.0442 < 5\%$, so significant. Significant	B1,B1 M1A1 M1
	There is evidence that the no. of family size bars sold is lower than usual.	A1 (6)
(b)	$H_0 : p = 0.02, H_1 : p \neq 0.02$ $\lambda = 4$ etc ok both Let Y represent the number of gigantic bars sold. $Y \sim B(200, 0.02) \Rightarrow Y \sim Po(4)$ can be implied below $P(Y = 0) = 0.0183$ and $P(Y \leq 8) = 0.9786 \Rightarrow P(Y \geq 9) = 0.0214$ first, either Critical region $Y = 0 \cup Y \geq 9$ $Y \leq 0$ ok N.B. Accept exact Bin: 0.0176 and 0.0202	B1 M1 B1,B1 B1,B1
(c)	Significance level = $0.0183 + 0.0214 = 0.0397$ awrt 0.04	B1 (1)
		Total 13

Question Number	Scheme	Marks
7. (a)	$1 - F(0.3) = 1 - (2 \times 0.3^2 - 0.3^3)$ = 0.847 ‘one minus’ required	M1 A1 (2)
(b)	$F(0.60) = 0.5040$ $F(0.59) = 0.4908$ both required awrt 0.5, 0.49 0.5 lies between therefore median value lies between 0.59 and 0.60.	M1A1 B1 (3)
(c)	$f(x) = \begin{cases} -3x^2 + 4x, & 0 \leq x \leq 1, \\ 0, & \text{otherwise.} \end{cases}$ attempt to differentiate, all correct	M1A1 (2)
(d)	$\int_0^1 xf(x)dx = \int_0^1 -3x^3 + 4x^2 dx$ $= \left[\frac{-3x^4}{4} + \frac{4x^3}{3} \right]_0^1$ attempt to integrate $xf(x)$ sub in limits	M1 M1 A1 (3)
(e)	$\frac{df(x)}{dx} = -6x + 4 = 0$ attempt to differentiate $f(x)$ and equate to 0 $x = \frac{2}{3}$ or 0.6 or 0.667	M1 A1 (2)
(f)	mean < median < mode, therefore negative skew. Any pair, cao	B1,B1 (2)
		Total 14