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Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓and x	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	
Other abbreviations	Meaning
in mark scheme	
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the question.

2. Subject-specific Marking Instructions for A Level Mathematics B (MEI)

- Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- In the units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Q	uestic	n	Answer	Marks	AOs	Guidance
1			-2	B1	1.1	
			5, –5	B1	1.1	Both needed
				[2]		
2			DR			
			$\begin{vmatrix} \mathbf{DK} \\ x^2 > 5x - 6 \end{vmatrix}$	M1	3.1a	
				M1	3.1a 1.1	
			$\begin{cases} x^2 - 5x + 6 > 0\\ (x - 2)(x - 3) > 0 \end{cases}$	A1	1.1	Correct factors or values 2, 3
						· I
			x < 2 or $x > 3$	A1	2.2a	oe, e.g. $\{x: x < 2 \cup x > 3\}$
				[4]		
3	(a)		5 million	B1	3.4	
3	(a)		3 minion	[1]	3.4	
3	(b)		The population is growing	B1	3.2a	
			At a rate proportional to the population	B1	3.2a	or at 2% a year
						or by the same percentage each
				[2]		year
3	(c)		DR	[2]		
	(C)		$5 \times 1.02^n = 10 \Rightarrow 1.02^n = 2$	M1	3.4	
				1,11		
			$n = \frac{\log 2}{\log 1.02} = 35.002$	M1	1.1a	oe
			2035	A1	3.2a	
			2000	[3]	3.2u	
3	(d)		$\log_{10} P = \log_{10} 5 + n \log_{10} 1.02$	M1	1.1	
				17:1		oe with clear link to gradient and
			Of form $y = mx + c$ [with $\log_{10} P$ as y and n as x]	E 1	2.4	intercept
				[2]		

(Question	Answer	Marks	AOs	Guidanc	e
4	(a)	[g(x) =]3x - 6	B1	2.2a		
			[1]			
4	(b)	$\left\{x:x\in j\ ,x\neq 2\right\}$	B1	1.1	oe; condone omission of $x \in i$	
			[1]			
4	(c)	Stretch	B 1	1.1	Allow these two marks	Transformation details
		Translation	B1	1.1	irrespective of the order of the transformations	not required here either
		Correct details for 1st transformation; can be any of	B1	1.1		
		(A) [stretch] parallel to x-axis scale factor $\frac{1}{3}$ or				
		(B) [stretch] parallel to y-axis scale factor $\frac{1}{3}$ or				Accept translation
		(C) [translation] 6 to the right or				details in column-
		(D) [translation] 2 to the right				vector form or in
		Correct details for 2nd transformation, which must correspond to the 1st transformation given:	B1	2.2a		equivalent words
		(A) [translation] 2 to the right or				
		(B) [translation] 2 to the right or				
		(C) [stretch] parallel to x-axis scale factor $\frac{1}{3}$ or				
		(D) [stretch] parallel to y-axis scale factor $\frac{1}{3}$				
			[4]			

Q	uestion	Answer	Marks	AOs	Guidance	
5		$u = 2x - 1 \Rightarrow \frac{\mathrm{d}u}{\mathrm{d}x} = 2$	M1	1.1a	oe	
		$\int_{5}^{15} \frac{u+1}{2u} \mathrm{d}u$	A1 B1	1.1 1.1	Integrand correct Limits correct (may be seen later or may later convert back to <i>x</i> instead)	
		$\frac{1}{2} \int_{5}^{15} \left(1 + \frac{1}{u} \right) \mathrm{d}u$	M1	1.1	Dividing through by <i>u</i>	Limits may be wrong
		$\frac{1}{2} \left[u + \ln u \right]_5^{15}$	A1	1.1	Integration correct, condone missing modulus sign and missing factor half	or missing for these two marks
		$\frac{1}{2} \left\{ 15 + \ln 15 - (5 + \ln 5) \right\} = \frac{1}{2} \left\{ 10 + \ln \left(\frac{15}{5} \right) \right\}$ $= 5 + \frac{1}{2} \ln 3$	E 1	2.1	AG Convincing correct completion	
		Alternative solution $\int_{3}^{8} \frac{2x}{2x-1} dx = \int_{3}^{8} \frac{2x-1+1}{2x-1} dx$ $\int_{3}^{8} \left(1 + \frac{1}{2x-1}\right) dx$	M1		oe attempt at algebraic division	Limits may be wrong or missing for these two marks
		$\left[x + \frac{1}{2}\ln 2x - 1 \right]_{3}^{8}$ $8 + \frac{1}{2}\ln 15 - \left(3 + \frac{1}{2}\ln 5\right)$	B1 B1		x and $\ln(2x-1)$ Factor $\frac{1}{2}$	Modulus not needed
		$8 + \frac{1}{2} \ln 15 - \left(3 + \frac{1}{2} \ln 5\right)$	M1		Correct substitution of limits	
		$5 + \frac{1}{2}\ln\left(\frac{15}{5}\right) = 5 + \frac{1}{2}\ln 3$	E 1		AG Convincing correct completion	
			[6]			

C)uestio	n	Answer	Marks	AOs	Guidance	
6	(a)		DR				
			$\frac{\mathrm{d}y}{\mathrm{d}x} = 1 + \ln x$	B1	1.1a	B1 for each term correct	
			$\frac{1}{dx} = 1 + \ln x$	B1	1.1	B1 for each term correct	
			At stationary point $\ln x = -1$	M1	1.1		
			$x = \frac{1}{2}$	A1	2.2a		
			$\begin{array}{c} x = - \\ e \end{array}$	AI	2.2a		
			1		2.2	(1 1)	
			$y = -\frac{1}{e}$	A1	2.2a	$\left(\frac{1}{e}, -\frac{1}{e}\right)$	
				[5]			
6	(b)		DR				
			$\frac{d^2y}{d^2}$	M1	110		
			$\frac{1}{dx^2} = \frac{1}{x}$	M1	1.1a		
						AG Convincing conclusion	
			At stationary point $\frac{d^2y}{dx^2}$ = e, positive so minimum	E1	2.4	needed	
			u.	[2]			

Q	uestio	n	Answer	Marks	AOs	Guidance	,
7	(a)		$0, 2\pi$	B1	1.2		
			π	B1 [2]	1.2		
7	(b)		$\csc^2 \theta = 1 + \cot^2 \theta$, so $\frac{2}{y} = 1 + \left(\frac{x}{2}\right)^2$	M1	3.1a		
			$\frac{2}{y} = \frac{4+x^2}{4}$ $y = \frac{8}{x^2+4}$	M1	1.1		
			$y = \frac{8}{x^2 + 4}$	A1	2.2a		
			Alternative solution 1				
			$x^2 = 4\cot^2\theta = \frac{4\cos^2\theta}{\sin^2\theta}$	M1			
			$x^2 = \frac{2(2-y)}{\frac{1}{2}y}$	M1			
			$y = \frac{8}{x^2 + 4}$	A1			
			Alternative solution 2				
			$\frac{A}{x^2 + B} = \frac{A}{4\cot^2\theta + B} = 2\sin^2\theta$	M1			
			$8\cos^2\theta + 2B\sin^2\theta = A$	M1			
			so $B = 4$ and $A = 8$, giving $y = \frac{8}{x^2 + 4}$	A1			
				[3]			
7	(c)		$\frac{8}{x^2 + 4} > 0 \text{ for all } x$	M1	2.1	or $2\sin^2\theta \ge 0$ and when $2\sin^2\theta = 0$, x is undefined	If zero scored, SC1 for $x^2 + 4$ is never
			So Ali is correct [because $y > 0$ for all x]	A1 [2]	2.3		negative oe

Q	uestic	n	Answer	Marks	AOs	Guidance
8	(a)		$-\frac{1}{x^2}\cos\left(\frac{1}{x}\right)$	B2	1.1a, 1.1	B1 for $-\frac{1}{x^2}$ or $\cos\left(\frac{1}{x}\right)$
				[2]		
8	(b)		$\frac{1}{x} > 0$	B1	2.2a	Correct lower limit 0 stated
			$\frac{1}{x} < \frac{\pi}{2}$	B1	2.2a	Correct upper limit $\frac{\pi}{2}$ stated
				[2]		
8	(c)		$0 < \frac{1}{x} < \frac{\pi}{2} \Rightarrow \cos\left(\frac{1}{x}\right) > 0$	M1	2.2a	
			$-\frac{1}{x^2} < 0$	M1	1.1	
			Hence $h'(x) < 0$ so $h(x)$ is a decreasing function	A1	2.4	AG Convincing completion needed
				[3]		

Q	uestic	n	Answer	Marks	AOs	Guidance	
9	(a)	(i)	DR dy 2				
			$\frac{\mathrm{d}y}{\mathrm{d}x} = 4x^2$	M1	1.1a		
			At point of contact, gradient = 1 so $4x^2 = 1$	E 1	2.4	AG Convincing completion needed	
0	(.)	(**)	DD	[2]			
9	(a)	(ii)	DR	D1	2.2	TO 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
			$x = \frac{1}{2}$	B1	3.2a	Taking the positive root	
			$y = \frac{1}{2}$	B 1	2.2a	soi	
			$\frac{1}{2} = \frac{4}{3} \left(\frac{1}{2}\right)^3 + a$	M1	3.1a		
			$a=\frac{1}{3}$	A1	1.1		
•			DD.	[4]			
9	(b)		DR When curve crosses line $\frac{4}{3}x^3 + \frac{1}{3} = x$	M1	3.1a		FT their (a), or
			$4x^3 - 3x + 1 = 0$	M1	1.1	oe; equation with zero on one side	working in terms of <i>a</i> , for all M marks
			$(2x-1)^2(x+1) = 0$	M1	2.2a		throughout this part
			x = -1	A1	1.1		
			$\int_{-1}^{\frac{1}{2}} \left(\frac{4}{3} x^3 + \frac{1}{3} - x \right) \mathrm{d}x$	M1	1.1	Need not include limits	
			$\int_{-1}^{\frac{1}{2}} \left(\frac{4}{3} x^3 + \frac{1}{3} - x \right) dx$ $\left[\frac{1}{3} x^4 + \frac{1}{3} x - \frac{1}{2} x^2 \right]_{-1}^{\frac{1}{2}}$	M1	1.1	Need not include limits	
			$\frac{9}{16}$	A1	1.1		
				[7]			

Q	Question		Answer	Marks	AOs	Guidance	
10	(a)		$\frac{16}{3}$ [units]	B1	2.2a	oe	
				[1]			
10	(b)		At each iteration, the perimeter is $\frac{4}{3}$ times the				
			previous perimeter	M1	3.1a	May be a specific instance	
			Perimeter of <i>n</i> th iteration = $3 \times \left(\frac{4}{3}\right)^n$	A2	1.1, 2.2a	Allow A1 for 3 times a power of $\frac{4}{3}$	
				[3]			
10	(c)		As $n \to \infty$, $3 \times \left(\frac{4}{3}\right)^n \to \infty$	E1	2.4	or $3 \times \left(\frac{4}{3}\right)^n$ increases without limit	
						as <i>n</i> increases	
				[1]			

11	(a)	Area of each little triangle = $\frac{1}{9}$ unit	M1	2.2a	or total additional area = $\frac{1}{3}$	
		Area = $1\frac{1}{3}$ [units]	A1	1.1		
			[2]			
11	(b)	$\frac{12}{81}$	B1	2.2a	oe	$\frac{4}{27}$
			[1]			
11	(c)	$1 + \frac{3}{9} + \frac{4 \times 3}{9 \times 9} + \frac{4 \times 4 \times 3}{9 \times 9 \times 9} + K$	M1 M1	3.1a 2.2a	4 times for new number of triangles Triangle area divided by 9	
		$1 + \frac{\frac{3}{9}}{1 - \frac{4}{9}}$	M1	3.1a	Use of GP formula	
		$\frac{8}{5}$ [units]	A1	1.1		
			[4]			

Question	Answer		AOs	Guidance	
12	e.g. 2 sticks of length $\sqrt{2}$	M1	3.1a	Correct number of sticks for the chosen stick length	
	e.g. 4 sticks of length 1	M1	2.1	Correct number of sticks for a different stick length	
	$D = -\frac{\ln 2}{\ln\left(\frac{1}{\sqrt{2}}\right)} = 2$	A1	1.1	AG Correct completion needed	
	, , <u>, , , , , , , , , , , , , , , , , </u>	[3]			

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