

# Practice Paper – Set 1

AS Level Mathematics B (MEI)

H630/01 Pure Mathematics and Mechanics

# MARK SCHEME

**Duration:** 1 hour 30 minutes

MAXIMUM MARK 70

Version: Final

Last updated: 04/12/17

This document consists of 14 pages

# **Text Instructions**

# 1. Annotations and abbreviations

| Annotation in scoris | Meaning  |
|----------------------|--|
| √and ×               |  |
| BOD                  | Benefit of doubt   |
| FT                   | Follow through   |
| ISW                  | Ignore subsequent working  |
| M0, M1               | Method mark awarded 0, 1   |
| A0, A1               | Accuracy mark awarded 0, 1   |
| B0, B1               | Independent mark awarded 0, 1  |
| SC                   | Special case   |
| ^                    | Omission sign  |
| MR                   | Misread  |
| Highlighting         |  |
|                      |  |
| Other abbreviations  | Meaning  |
| in mark scheme       |  |
| E1                   | Mark for explaining a result or establishing a given result  |
| dep*                 | Mark dependent on a previous mark, indicated by *  |
| cao                  | Correct answer only  |
| oe                   | Or equivalent  |
| rot                  | Rounded or truncated   |
| soi                  | Seen or implied  |
| www                  | Without wrong working  |
| AG                   | Answer given   |
| awrt                 | Anything which rounds to   |
| BC                   | By Calculator  |
| DR                   | This indicates that the instruction In this question you must show detailed reasoning appears in the question. |

### 2. Subject-specific Marking Instructions for AS Level Mathematics B (MEI)

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

# Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

#### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

# В

Mark for a correct result or statement independent of Method marks.

#### Е

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is

worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.
- k Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned on this occasion, but shows what a complete solution might look like.

#### I. Crossed Out Responses

Where a candidate has crossed out a response and provided a clear alternative then the crossed out response is not marked. Where no alternative response has been provided, examiners may give candidates the benefit of the doubt and mark the crossed out response where legible.

Contradictory Responses

When a candidate provides contradictory responses, then no mark should be awarded, even if one of the answers is correct.

#### m. Award No Response (NR) if:

• there is nothing written in the answer space.

Award Zero '0' if:

• anything is written in the answer space and is not worthy of credit (this includes text and symbols).

Team Leaders must confirm the correct use of the NR button with their markers before live marking commences and should check this when reviewing scripts.

| Q | <b>Juestion</b> | Answer                                    | Marks | AOs  | Guidance                                     |
|---|-----------------|---|-------|------|--|
| 1 |                 | $2\theta = \cos^{-1} 0.3$                 | M1    | 1.1a |  |
|   |                 | $2\theta = 72.54, 287.46, 432.54, 647.46$ |       |      |  |
|   |                 | $\theta$ = 36.3, 143.7, 216.3, 323.7      | A1    | 1.1b | For at least one correct answer in the range |
|   |                 |   | A1    | 1.1b | For all correct with no others in the range  |
|   |                 |   | [3]   |      |  |

| 2 | Boundary values –2, 7                   | B1        | 3.1a | BC  |  |
|---|---|-----------|------|---|--|
|   | $\{x : x \le -2\} \cup \{x : x \ge 7\}$ | B1        | 2.3  | For both of $x < -2$ , $x > 7$ or better                        | Ignore use of either<br>'or' or 'and' here |
|   |   | <b>B1</b> | 2.5  | For completely correct answer expressed in correct set notation | Must be $\leq$ and $\geq$ for this mark    |
|   |   | [3]       |      |   |  |

| 3 | Let $T_1$ and $T_2$ be the tensions in the strings to <i>m</i> kg mass<br>and $2m$ kg mass respectively |            |      |  |  |
|---|---|------------|------|--|--|
|   | $T_1 = mg$ and $T_2 = 2mg$  | <b>B</b> 1 | 3.3  | For values of tensions clearly stated or<br>shown on the diagram |  |
|   | $T_2 - T_1 - F = 0$   | M1         | 3.3  |  |  |
|   | F = mg towards the <i>m</i> kg mass (to the left on the diagram)  | A1         | 2.2a |  |  |
|   |   | [3]        |      |  |  |

| ( | Question | Answer  | Marks      | AOs          | Guidance   |  |
|---|----------|---|------------|--------------|--|--|
| 4 | (i)      | Distance $CO = \sqrt{(-4)^2 + 3^2} = 5$       | M1         | 1.1a         | Allow $(-4)^2 + 3^2$ if CO <sup>2</sup> clearly stated |  |
|   |          | $(x+4)^2 + (y-3)^2 = 25$                      | M1         | 1.1a         | Use of circle equation with their $r^2$                |  |
|   |          |   | A1         | 2.1          | Correct answer; isw                                    |  |
|   |          |   | [3]        |              |  |  |
|   | (ii)     | A is the point (0, 6)                         | <b>B</b> 1 | <b>3.1</b> a |  |  |
|   |          | Gradient of AC is $\frac{3}{4}$               | M1         | 1.1a         |  |  |
|   |          | Gradient of tangent is $-\frac{4}{3}$         | M1         | 1.1a         |  |  |
|   |          | [Equation of tangent is $y-6=-\frac{4}{3}x$ ] |            |              |  |  |
|   |          |   | M1FT       | 1.1b         | Use their point A and gradient to find B               |  |
|   |          | When $y = 0, \ x = \frac{9}{2}$               | A1         | 2.2a         | cao  |  |
|   |          |   | [5]        |              |  |  |
|   | ,        |   |            |              |  |  |
| 5 |          | Use of $n + 1$ and $n - 1$                    | B1         | 2.1          | For both expressions seen                              |  |
|   |          | $(n+1)(n-1) = n^2 - 1$                        | M1         | <b>1.1</b> a | Must be multiplied with attempt to expand              |  |

|  | $(n+1)(n-1) = n^2 - 1$  | M1         | 1.1a | Must be multiplied with attempt to expand brackets |  |
|--|---|------------|------|--|--|
|  | Therefore (the conjecture is) true for all positive integers $n$ (greater than 1) | <b>E</b> 1 | 2.1  | Clear conclusion must be stated                    |  |
|  |   | [3]        |      |  |  |

| Q | uestion | Answer   | Marks     | AOs  | Guidance  |
|---|---------|--|-----------|------|---|
| 6 | (i)     | DR   |           |      |   |
|   |         | $v = -0.7 \times 2t + 4$                                   | M1        | 3.1b | For attempt to differentiate  |
|   |         | When $t = 7$ , $v = -5.8$                                  | M1        | 3.4  | For substitution in their v   |
|   |         | Boy is moving due south since $v$ is negative              | <b>E1</b> | 2.2a | Dependent on correct -5.8   |
|   |         |  | [3]       |      |   |
|   | (ii)    | DR   |           |      |   |
|   |         | Max/min <i>s</i> when $v = 0$ , so $-1.4t + 4 = 0$         | M1        | 3.1b | For attempt to solve their $v = 0$  |
|   |         | $t = \frac{20}{7}$   | A1        | 1.1b |   |
|   |         | When $t = \frac{20}{7}$ , $s = \frac{40}{7} = 5.71$ to 3sf | A1FT      | 1.1b | Follow through their <i>t</i>   |
|   |         | When $t = 10$ , $s = -30$ and when $t = 0$ , $s = 0$       | <b>B1</b> | 1.1b | For checking both end-points  |
|   |         | Greatest distance is 30 m                                  | B1FT      | 3.2a | Must select (their) correct distance, must<br>be positive and must have units |
|   |         |  | [5]       |      |   |

| Q | uestion       | n Answer  | Marks     | AOs          | Guidance  |
|---|---------------|---|-----------|--------------|---|
| 7 | (i)           |   |           |              |   |
|   |               | $\mathbf{a} = 5\mathbf{i} + 6\mathbf{j}$  | M1        | 1.1a         | Using vector notation   |
|   |               | $\overrightarrow{OC} = \overrightarrow{OB} + \overrightarrow{BC} = \overrightarrow{OB} + \overrightarrow{OA} = \mathbf{b} + \mathbf{a}$       | M1        | <b>3.1</b> a | Using <b>a</b> for vector $\overrightarrow{BC}$ in an addition                              |
|   |               | = (5i + 6j) + (-2i - 7j) = 3i - j   |           |              |   |
|   |               | So C is (3, -1)   | <b>E1</b> | 3.2a         | Must be coordinates; do not allow for<br>position vector only                               |
|   |               |   | [3]       |              |   |
|   | ( <b>ii</b> ) | $\overrightarrow{OM} = \frac{1}{2}(\mathbf{a} + \mathbf{b}) = \frac{3}{2}\mathbf{i} - \frac{1}{2}\mathbf{j}$                                  | B1        | 2.1          |   |
|   |               | $\overline{\mathrm{MC}} = (3\mathbf{i} - \mathbf{j}) - \left(\frac{3}{2}\mathbf{i} - \frac{1}{2}\mathbf{j}\right)$                            | <b>M1</b> | 1.1a         |   |
|   |               | $=\left(\frac{3}{2}\mathbf{i}-\frac{1}{2}\mathbf{j}\right)=\overline{\mathbf{OM}}$  | A1        | 2.1          |   |
|   |               |   | [3]       |              |   |
|   | (iii)         | $\left  \overrightarrow{\mathrm{MC}} \right  = \left  \frac{3}{2}\mathbf{i} - \frac{1}{2}\mathbf{j} \right  = \frac{1}{2}\sqrt{3^2 + (-1)^2}$ | M1        | <b>1.1</b> a | Or exact equivalent, e.g. $\sqrt{\left(\frac{3}{2}\right)^2 + \left(-\frac{1}{2}\right)^2}$ |
|   |               | $=\frac{1}{2}\sqrt{10}$   | A1        | 1.1b         | Accept alternative answer $\sqrt{\frac{5}{2}}$  |
|   |               |   | [2]       |              |   |

| Q | uestion | Answer  | Marks | AOs          | Guidance  |
|---|---------|---|-------|--------------|---|
| 8 |         | DR  |       |              |   |
|   |         | Consider $\int_{-1}^{0} x^3(x-3) dx$ and $\int_{0}^{3} x^3(x-3) dx$   | M1    | <b>3.1</b> a | Splitting the integral into positive and negative regions with correct limits |
|   |         | $\int x^3 (x-3)  \mathrm{d}x = \int (x^4 - 3x^3)  \mathrm{d}x$  | M1    | <b>1.1</b> a | Attempting to integrate expanded form   |
|   |         | $\frac{x^5}{5} - \frac{3x^4}{4}(+c)$  | A1    | 1.1a         | Correct indefinite integral seen  |
|   |         | $\left[\frac{x^5}{5} - \frac{3x^4}{4}\right]_{-1}^0 = 0 - \left(\frac{(-1)^5}{5} - \frac{3(-1)^4}{4}\right) = \frac{19}{20}$  | A1    | 1.1b         | Must be seen to use limits  |
|   |         | $\left[\frac{x^5}{5} - \frac{3x^4}{4}\right]_0^3 = \left(\frac{3^5}{5} - \frac{3 \times 3^4}{4}\right) - 0 = -\frac{243}{20}$ | A1    | 1.1b         | Must be seen to use limits  |
|   |         | $\frac{19}{20} + \frac{243}{20} = \frac{131}{10}$   | B1    | 1.1b         | www; not dependent on previous marks  |
|   |         |   | [6]   |              |   |

| Q | Question | Answer   | Marks      | AOs          | Guidance  |
|---|----------|--|------------|--------------|---|
| 9 | (i)      |  | G1         | 1.2          | Correct shape with x-axis as asymptote                |
|   |          | 2 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -1             | G1         | 1.2          | (0, 1) clearly shown                                  |
|   |          |  | [2]        |              |   |
|   | (ii)     | Stretch in the <i>x</i> -direction                   | B1         | <b>1.1</b> a | 'Stretch' must be seen at least once for any          |
|   |          | Stretch scale factor $\frac{1}{2}$                   | <b>B</b> 1 | 1.1a         | marks to be awarded, but the word needn't be repeated |
|   |          |  | [2]        |              |   |
|   | (iii)    | $\frac{\mathrm{d}y}{\mathrm{d}x} = 2\mathrm{e}^{2x}$ | M1         | 1.1a         | Allow for any $ke^{2x}$                               |
|   |          |  | A1         | 1.1b         | Correct $2e^{2x}$                                     |
|   |          | When $x = 3$ , $\frac{dy}{dx} = 2e^6$                | A1         | 1.1a         |   |
|   |          | and $y = e^6$  | B1         | <b>1.1</b> a |   |
|   |          | Tangent is $y - e^6 = 2e^6(x-3)$                     | M1         | <b>1.1</b> a | Allow method if 403 or better used for $e^6$          |
|   |          | $y = 2e^6x - 5e^6$                                   |            |              |   |
|   |          | $y = e^6(2x - 5)$                                    | A1         | 2.1          | Must be in this form                                  |
|   |          |  | [6]        |              |   |

| Questi | on Answer   | Marks      | AOs          | Guidance   |
|--------|---|------------|--------------|--|
| 10     | 90 + 90 - 170 = 20a   | M1         | 3.3          | For use of Newton II                                       |
|        | a = 0.5   | A1         | 1.1b         |  |
|        | $3 = 0 + \frac{1}{2} \times 0.5t^2$ $t = \sqrt{12}$                     | M1         | <b>1.1</b> a | For use of <i>suvat</i> with $s = 3$ and $u = 0$           |
|        | $t = \sqrt{12}$   | A1         | 1.1b         | 3.464  |
|        | $v = 0 + 0.5\sqrt{12}$  | M1         | 3.4          | For use of <i>suvat</i> with their $a$ and $t$ to find $v$ |
|        | $=\sqrt{3}$   | A1         | 1.1b         | 1.732  |
|        | In second phase resultant force is zero so $a = 0$                      | <b>B</b> 1 | 3.3          | Allow for 'constant speed' seen                            |
|        | Time at constant speed $=\frac{7}{\sqrt{3}}$                            | M1         | 1.1a         |  |
|        | Total time = $2\sqrt{3} + \frac{7\sqrt{3}}{3} = 3.464 + 4.041 = 7.51 s$ | A1         | 1.1b         |  |
|        | (3sf)   |            |              |  |
|        |   | [9]        |              |  |

| Q  | uestion       | Answer  | Marks | AOs          | Guidance  |                                  |
|----|---------------|---|-------|--------------|---|----------------------------------|
| 11 | (i)           | b = 80  | B1    | 1.2          |   |                                  |
|    |               | c = 10  | B1    | 3.3          |   |                                  |
|    |               |   | [2]   |              |   |                                  |
|    | ( <b>ii</b> ) | $12 = a(30 - 80)^2 + 10$  | M1    | 3.3          | Substituting $v = 30$ , $y = 12$ in the model with their values for <i>b</i> and <i>c</i>                                   |                                  |
|    |               | $a = \frac{2}{50^2} = 0.0008$   | A1    | 1.1b         |   |                                  |
|    |               |   | [2]   |              |   |                                  |
|    | (iii)         | When $v = 110$ , $y = 0.0008(110 - 80)^2 + 10$  | M1    | 3.4          | Substitution in the model with their values for $a, b$ and $c$  |                                  |
|    |               | y = 10.72   | A1    | 1.1b         |   |                                  |
|    |               |   | [2]   |              |   |                                  |
|    | (iv)          | 14 y  | G1    | <b>1.1</b> a | Curve with minimum point at (80, 10)  | Condone graph continuing outside |
|    |               |   | G1    | <b>1.1</b> a | End-points (30, 12) and (110, 10.72)  | the given interval               |
|    |               |   | [2]   |              |   |                                  |
|    | ( <b>v</b> )  | A quadratic model giving the same value at $v = 30$ and $v = 110$ would have to have the minimum point halfway between, at $v = 70$ , by symmetry This is not the case so a quadratic model is not suitable | E1    | 3.5b         | Accept equivalent statement involving<br>symmetry, or any other sensible argument<br>referring to relevant numerical values |                                  |
|    |               |   | [1]   |              |   |                                  |