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Mark Scheme

June 2014

Question		Answer	Marks	Guidance
1	(i)	$\frac{1}{9}$	2 [2]	isw conversion to decimal M1 for 9 or for 3^{-2} or for $\frac{1}{3}$ Except M0 for 9 from $27/3$ or $\sqrt[3]{27}$ ie M1 for evidence of $(\sqrt[3]{27})^2$ or $1/(\sqrt[3]{27})$ found correctly
1	(ii)	$2a^2c^{-4}$ or $\frac{2a^2}{c^4}$ as final answer	3 [3]	B1 for each element; must be multiplied if B0, allow SC1 for $64a^6c^3$ obtained from numerator or for all elements correct but added
2		midpt M of AB = $\left(\frac{1+6}{2}, \frac{5-1}{2}\right)$ oe isw soi subst of their midpt into $y = 2x - 5$ and attempting to evaluate all work correct and 'Yes' oe	M1 M1 A1 [3]	condone lack of brackets; accept in the form $x = 7/2$ oe, $y = 2$ oe eg $2 \times$ their $3.5 - 5 =$ their result accept $2 = 2 \times 3.5 - 5$ <u>alt methods</u> : allow 2 nd M1 for finding correct eqn of AB as $y = -\frac{6x}{5} + \frac{31}{5}$ oe <u>and</u> attempting to solve as simlt eqn with $y = 2x - 5$ for x or y or allow M1 for finding in unsimplified form the eqn of the line through their midpt with gradient 2 and A1 for showing it is $y = 2x - 5$, so Yes

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3	(i)	graph of shape with vertices at $(-2, -3)$, $(0, 0)$ and $(2, -4)$	2 [2]	M1 for 2 vertices correct	condone lines unruled; condone just missing vertex: $\frac{1}{4}$ grid square tolerance
3	(ii)	graph of shape with vertices at $(1, -1)$, $(3, 2)$ and $(5, -2)$	2 [2]	M1 for 2 vertices correct or for shape with vertices at $(-5, -1)$, $(-3, 2)$ and $(-1, -2)$	condone lines unruled; condone just missing vertex: $\frac{1}{4}$ grid square tolerance
4	(i)	$61 - 28\sqrt{3}$	3 [3]	B2 for 61 or B1 for $49 + 12$ found in expansion (may be in a grid) and B1 for $-28\sqrt{3}$ if B0, allow M1 for at least three terms correct in $49 - 14\sqrt{3} - 14\sqrt{3} + 12$ the correct answer obtained then spoilt earns SC2 only	
4	(ii)	$4\sqrt{3}$	2 [2]	M1 for $\sqrt{50} = 5\sqrt{2}$ or $\sqrt{300} = 10\sqrt{3}$ or $20\sqrt{300} = 200\sqrt{3}$ or $\sqrt{48} = 2\sqrt{12}$ seen	

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5		$3a + 12 [= ac + 5f]$	M1	for expanding brackets correctly	annotate this question if partially correct ft only if two a terms ft only if two a terms, needing factorising may be earned before 2 nd M1
		$3a - ac = 5f - 12$ or ft	M1	for collecting a terms on one side, remaining terms on other	
		$a(3 - c) = 5f - 12$ or ft	M1	for factorising a terms; may be implied by final answer	
		$[a =] \frac{5f - 12}{3 - c}$ oe or ft as final answer	M1	for division by their two-term factor; for all 4 marks to be earned, work must be fully correct	
			[4]		
6		$(3x + 1)(x + 3)$	M1	or $3(x + 1/3)(x + 3)$	A0 for combinations with only one part correct eg $-3 > x < -1/3$, though this would earn M1 if not already awarded
		$x < -3$	A1	or for $-1/3$ and -3 found as endpoints eg by use of formula	
		[or]			
		$x > -1/3$ oe	A1	mark final answers;	
				allow only A1 for $-3 > x > -1/3$ oe as final answer or for $x \leq -3$ and $x \geq -1/3$	
				if M0, allow SC1 for sketch of parabola the right way up with their solns ft their endpoints	
			[3]		

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7		70 000 www	4	<p>throughout, condone xs included eg $(2x)^4$</p> <p>allow 4 for $70\,000x^4$ www;</p> <p>may also include other terms in expansion. Allow marks even if wrong term selected; mark the coefficient of x^4</p> <p>may be unsimplified, but do not allow 35 in factorial form unless evaluated later</p> <p>or for all three elements seen together (eg in table) but not multiplied</p> <p>M3 for $35 \times 5^3 \times 2^4$ oe</p> <p>or M2 for two of these elements multiplied</p> <p>or M1 for 35 oe or for 1 7 21 35 35 21 7 1 row of Pascal's triangle seen</p>
			[4]	

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8		<p>use of $f(2)$</p> <p>$4 \times 2^3 + 2k + 6 = 42$</p> <p>$k = 2$</p> <p>$[x =] -1$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[4]</p>	<p>2 substituted in $f(x)$ or $f(2) = 42$ seen or correct division of $4x^3 + kx + 6$ by $x - 2$ as far as obtaining $4x^2 + 8x + (k + 16)$ oe [may have $4x^2 + 8x + 18$]</p> <p>or $6 + 2(k + 16) = 42$ oe</p> <p>or finding (usually after division) that the constant term is 36 and then working with the x term to find k eg $kx + 16x = 18x$</p> <p>as their answer, not just a trial;</p> <p>A0 for just $f(-1) = 0$ with no further statement</p> <p>A0 if confusion between roots and factors in final statement eg '$x + 1$ is a root', even if they also state $x = -1$</p>

accept with no working since it can be found by inspection

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9	(i)	$3n^2 + 6n + 5$ isw	B2 [2]	M1 for a correct expansion of at least one of $(n + 1)^2$ and $(n + 2)^2$	
9	(ii)	odd numbers with valid explanation	B2 [2]	<p>marks dep on 9(i) correct or starting again</p> <p>for B2 must see at least odd \times odd = odd [for $3n^2$] (or when n is odd, $[3]n^2$ is odd) and odd [+ even] + odd = even soi,</p> <p>condone lack of odd \times even = even for $6n$; condone no consideration of n being even</p> <p>or B2 for deductive argument such as: $6n$ is always even [and 5 is odd] so $3n^2$ must be odd so n is odd</p> <p>B1 for odd numbers with a correct partial explanation or a partially correct explanation</p> <p>or B1 for an otherwise fully correct argument for odd numbers but with conclusion positive odd numbers or conclusion negative odd numbers</p> <p>B0 for just a few trials and conclusion</p>	<p>accept a full valid argument using odd and even from starting again</p> <p>Ignore numerical trials or examples in this part – only a generalised argument can gain credit</p>

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10	(i)	(7, 0)	1 [1]	accept $x = 7, y = 0$ condone 7, 0
10	(ii)	$\sqrt{13}$ $(x - 4)^2 + (y - 2)^2 = 13$ or ft their evaluated r^2 , isw	2 2 [4]	M1 for Pythagoras used correctly eg [$r^2 =$] $3^2 + 2^2$ or for subst A or their B in $(x - 4)^2 + (y - 2)^2 [= r^2]$ or B1 for [$r =$] $\pm\sqrt{13}$ M1 for one side correct, as part of an equation with x and y terms do not accept $(\sqrt{13})^2$ instead of 13; allow M1 for LHS for $(x - 4)^2 + (y - 2)^2 = r^2$ (or worse, $(x - 4)^2 + (y - 2)^2 = r$) (may be seen in attempt to find radius)
10	(iii)	(7, 4)	2 [2]	B1 each coord accept $x = 7, y = 4$ if B0, then M1 for a vector or coordinates approach such as '3 along and 2 up' to get from A to C oe or M1 for $\frac{x_D + 1}{2} = 4$ and $\frac{y_D + 0}{2} = 2$ condone 7, 4 or M1 for longer method, finding the equation of the line CD as $y = \frac{2}{3}(x - 1)$ oe <u>and</u> then attempting to find intrn with their circle

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10	(iv)	grad tgt = $-3/2$ oe	M2	correctly obtained or ft their D if used	annotate this question if partially correct may use AD, CD or AC NB grad AD etc may have been found in part (iii); allow marks if used in this part – mark the copy of part (iii) that appears below the image for part (iv) condone $y = \frac{-3x + 29}{2}$ condone $y = -1.5x + b$ and $b = 14.5$ oe
		$y - \text{their } 4 = \text{their } (-3/2)(x - \text{their } 7)$	M1	or subst (7, 4) into $y = \text{their } (-3/2)x + b$	
		$y = -1.5x + 14.5$ oe isw	A1	must be in form $y = ax + b$	
			[4]		

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11	(i)	$x = 4$ $(4, -3)$	B1 B1 [2]	or $x = 4, y = -3$ condone 4, -3
11	(ii)	$(0, 13)$ isw [when $y = 0,$] $(x - 4)^2 = 3$ $[x =] 4 \pm \sqrt{3}$ or $\frac{8 \pm \sqrt{12}}{2}$ isw	1 M1 A2 [4]	or [when $x = 0,$] $y = 13$ isw 0 for just $(13, 0)$ or $(k, 13)$ where $k \neq 0$ or $x^2 - 8x + 13 [= 0]$ need not go on to give coordinate form A1 for one root correct allow M1 for $y = x^2 - 8x + 13$ only if they go on to find values for x as if y were 0 annotate this question if partially correct may be implied by correct value(s) for x found
11	(iii)	replacement of x in their eqn by $(x - 2)$ completion to given answer $y = x^2 - 12x + 33,$ showing at least one correct interim step	M1 A1 [2]	may be simplified; eg $[y =] (x - 6)^2 - 3$ or allow M1 for $(x - 6 - \sqrt{3})(x - 6 + \sqrt{3})$ [$=0$ or y] cao; condone using $f(x - 2)$ in place of y condone omission of 'y =' for M1, but must be present in final line for A1

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11	(iv)	$x^2 - 12x + 33 = 8 - 2x$ or $(x - 6)^2 - 3 = 8 - 2x$	M1	for equating curve and line; correct eqns only; or for attempt to subst $(8 - y)/2$ for x in $y = x^2 - 12x + 33$	annotate this question if partially correct allow $\frac{10 \pm \sqrt{0}}{2}$ oe if $b^2 - 4ac = 0$ is not used explicitly A0 for $(x - 5)^2 = y$ allow recovery from $(x - 5)^2 = y$ examiners: use one mark scheme or the other, to the benefit of the candidate if both methods attempted, but do not use a mixture of the schemes condone no further interim step if all working in this part is correct so far
		$x^2 - 10x + 25 = 0$	M1	for rearrangement to zero, condoning one error such as omission of '='	
		$(x - 5)^2 [= 0]$	A1	or showing $b^2 = 4ac$	
		$x = 5$ www [so just one point of contact]	A1	may be part of coordinates $(5, k)$	
		point of contact at $(5, -2)$	A1	dependent on previous A1 earned; allow for $y = -2$ found	
		<u>alt. method</u>	or		
		for curve, $y' = 2x - 12$	M1		
		$2x - 12 = -2$	M1	for equating their y' to -2	
		$x = 5$, and y shown to be -2 using eqn to curve	A1		
		tgt is $y + 2 = -2(x - 5)$	A1		
deriving $y = 8 - 2x$	A1				
			[5]		

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12	(iii)	<p>ruled line drawn through $(-2, 0)$ and $(0, 10)$ and long enough to intersect curve at least twice</p> <p>-5.3 to -5.4 and 1.8 to 1.9</p>	<p>B1</p> <p>B2</p> <p>[3]</p>	<p>tolerance half a small square on grid at $(-2, 0)$ and $(0, 10)$</p> <p>B1 for one correct ignore the solution -2 but allow B1 for both values correct but one extra or for wrong 'coordinate' form such as $(1.8, -5.3)$</p> <p>insert BP on spare copy of graph if not used, to indicate seen – this is included as part of image, so scroll down to see it accept in coordinate form ignoring any y coordinates given;</p>
12	(iv)	<p>$2x^3 + 11x^2 - x - 30 = 5x + 10$</p> <p>$2x^3 + 11x^2 - 6x - 40 [= 0]$</p> <p>division by $(x + 2)$ and correctly obtaining $2x^2 + 7x - 20$</p> <p>substitution into quadratic formula or for completing the square used as far as</p> <p>$x + \frac{7}{4} = \frac{209}{16}$ oe</p> <p>$[x =] \frac{-7 \pm \sqrt{209}}{4}$ oe isw</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>for equating curve and line; correct eqns only</p> <p>for rearrangement to zero, condoning one error</p> <p>or showing that $(x + 2)(2x^2 + 7x - 20) = 2x^3 + 11x^2 - 6x - 40$, with supporting working</p> <p>condone one error eg a used as 1 not 2, or one error in the formula, using given $2x^2 + 7x - 20 = 0$</p> <p>dependent only on 4th M1</p> <p>annotate this question if partially correct</p>