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## Mark Scheme

June 2015

Question		Answer	Marks	Guidance
1		$[r =] \sqrt{\frac{A}{\pi(x+y)}}$ or $[r =] \sqrt{\frac{A}{\pi x + \pi y}}$ as final answer	2            <b>[2]</b>	square root symbol must extend below fraction line; accept to power $\frac{1}{2}$ with appropriate brackets  <b>M1</b> for a triple decker fraction or for $r^2 = \frac{A}{\pi(x+y)}$ or for $[r =] \pm \sqrt{\frac{A}{\pi(x+y)}}$ or for their final answer for $r$ ft their $r^2$  condone missing end bracket in denominator  eg M1 for $[r =] \sqrt{\frac{A}{\pi(x+y)}}$
2		$y = 4x + 10$            (0, 10) or ft            (-10/4, 0) oe or ft	B3            B1            B1            <b>[5]</b>	<b>M1</b> for $y = 4x + b$ oe  and <b>M1</b> for $y - 6 = \text{their } a(x + 1)$ oe or for $(-1, 6)$ subst in $y = (\text{their } a)x + b$ oe  or <b>M1</b> for $y = ax + 10$  condone $y = 10$ isw            condone $x = -10/4$ isw            condone lack of brackets and eg $y = 10, x = -2.5$ or ft isw  but B0, SC1 for poor notation such as $(-2.5, 10)$ with no better answers seen  Throughout the scheme, note that for evaluated rational answers, unless specified otherwise, fractional or decimal equivalents are acceptable, but not triple-decker fractions etc; integer answers must be simplified to an integer

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3	(i)	1	1 [1]		
3	(ii)	$\frac{3}{5}$ or 0.6	3       [3]	allow <b>B3</b> for $\pm 0.6$ oe;  <b>M1</b> for $\left(\frac{25}{9}\right)^{\frac{1}{2}} = \left(\frac{9}{25}\right)^{\frac{1}{2}}$ soi or $\frac{1}{\left(\frac{25}{9}\right)^{\frac{1}{2}}}$  and <b>M1</b> for at least one of 3 and 5 found	M1 for inversion even if they have done something else first, eg may be earned after 2 <sup>nd</sup> M1 for inversion of their $\frac{5}{3}$
4		$4x - 5 > 14x + 7$  $-12 > 10x$ or $-10x > 12$ or ft  $x < -\frac{12}{10}$ or $-\frac{12}{10} > x$ oe isw or ft	M1  M1  M1  [3]	for correctly multiplying by 7 to eliminate the fraction, including expanding bracket if this step done first  for correctly collecting $x$ terms on one side and number terms on the other and simplifying  ft their $ax$ [inequality] $b$ , where $b \neq 0$ and $a \neq 0$ or $\pm 1$	may be earned later; the first two Ms may be earned with an equation or wrong inequality  ft wrong first step  award 3 marks only if correct answer obtained after equations or inequalities are used with no errors
5		$x + 3(5x - 2) = 8$ or $y = 5(8 - 3y) - 2$  $16x = 14$ or $16y = 38$  (7/8, 19/8) oe	M1  M1  A2  [4]	for subst to eliminate one variable; condone one error;  for collecting terms and simplifying; condoning one error ft  or $x = 14/16$ , $y = 38/16$ oe isw allow <b>A1</b> for each coordinate	or multn or divn of one or both eqns to get a pair of coeffts the same, condoning one error  appropriate addn or subtn to eliminate a variable, condoning an error in one term; if subtracting, condone eg $y$ instead of 0 if no other errors



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8	(i)	$(3x)^2 = h^2 + (2x + 1)^2$ oe	B1	for a correct Pythagoras statement for this triangle, in terms of $x$ , with correct brackets	condone another letter instead of $h$ for one mark but not both unless recovered at some point
		$9x^2 = h^2 + 4x^2 + 4x + 1$ and completion to given answer, $h^2 = 5x^2 - 4x - 1$	B1	for correct expansion, with brackets or correct signs; must complete to the given answer with no errors in any interim working  may follow $3x^2 = h^2 + (2x + 1)^2$ oe for <b>B0 B1</b>	eg B1 for $h^2 = 9x^2 - (4x^2 + 4x + 1)$ and completion to correct answer but B0 for $h^2 = 9x^2 - 4x^2 + 4x + 1$
8	(ii)	$[0 =] 5x^2 - 4x - 8$	B1	for subst and correctly rearranging to zero	or M1 for $\left(x - \frac{2}{5}\right)^2 = \left(\frac{2}{5}\right)^2 + \frac{8}{5}$ oe, (condoning one error), which also implies first M1 if not previously earned  M0 for factorising ft
		$\frac{4 \pm \sqrt{(-4)^2 - 4 \times 5 \times -8}}{2 \times 5}$ or ft	M1	for use of formula in their eqn rearranged to zero, condoning one error; ft only if their rearranged eqn is a 3-term quadratic; no ft from $5x^2 - 4x - 1 [ = 0 ]$	
		$\frac{4 + \sqrt{176}}{10}$ or $\frac{2}{5} + \frac{\sqrt{44}}{5}$ oe	A1	isw wrong simplification;  <b>A0</b> if negative root also included	
			<b>[3]</b>		
9	(i)	the diagonals of a rhombus also intersect at $90^\circ$	B1	oe for kite or other valid statement/sketch  <b>B0</b> if eg rectangle or parallelogram etc also included as having diagonals intersecting at $90^\circ$	accept 'diamond' etc  reference merely to 'other shapes' having diagonals intersecting at $90^\circ$ is not sufficient; sketches must have diagonals drawn, intersecting approx. at right angles but need not be ruled
		ABCD is a square $\Rightarrow$ the diagonals of quadrilateral ABCD intersect at $90^\circ$	B1	oe; <b>B0</b> if no attempt at explanation (explanation does not need to gain a mark)	Do not accept $\rightarrow$ oe
			<b>[2]</b>		

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9	(ii)	eg 8 is an integer but $\sqrt{8}$ is not an integer	B1	oe with another valid number, or equivalent explanation	0 for 'the square root of some integers is a fraction'  Do not accept $\leftarrow$ oe
		$x^2$ is an integer $\Leftarrow x$ is an integer	B1	<b>B1</b> for the square root of some integers is a surd / irrational number / decimal  <b>B0</b> if no attempt at explanation	
10	(i)	graph of cubic correct way up	B1	<b>B0</b> if stops at $x$ -axis	must not have any ruled sections; no curving back; condone slight 'flicking out' at ends but not approaching a turning point; allow max on $y$ -axis or in 1st or 2nd quadrants; condone some 'doubling' or 'feathering' (deleted work still may show in scans)  allow if no graph, but marked on $x$ -axis condone intercepts for $x$ and / or $y$ given as reversed coordinates  allow if no graph, but eg B0 for graph with intn on $y$ -axis nowhere near their indicated 30
		crossing $x$ -axis at $-3, 2$ and $5$	B1	on graph or nearby; may be in coordinate form  mark intent for intersections with both axes	
		crossing $y$ -axis at $30$	B1	or $x = 0, y = 30$ seen if consistent with graph drawn	
			[2]		
10	(ii)	correct expansion of two of the linear factors	M1	may be 3 or 4 terms	condone lack of brackets if correct expansions as if they were there  or for direct expansion of all three factors, allow M1 for $x^3 + 3x^2 - 2x^2 - 5x^2 - 6x - 15x + 10x + 30$ , condoning an error in one term, and A1 if no error for completion by stating given answer
		correct expansion and completion to given answer, $x^3 - 4x^2 - 11x + 30$	A1	must be working for this step before given answer	
			[2]		

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10	(iii)	translation	B1	0 for shift or move etc without stating translation	0 if eg stretch also mentioned
		$\begin{pmatrix} 0 \\ -36 \end{pmatrix}$	B1	or 36 down, or $-36$ in y direction oe	if conflict, eg between ' $-36$ in y direction' and wrong vector, award B0  0 for ' $-36$ down'
10	(iv)	$-1 - 4 + 11 - 6 = 0$  attempt at division by $(x + 1)$ as far as $x^3 + x^2$ in working  correctly obtaining $x^2 - 5x - 6$  factorising the correct quadratic factor $x^2 - 5x - 6$ , that has been correctly obtained  $(x - 6)(x + 1)^2$ oe isw	B1  M1  A1  M1    A1	or <b>B1</b> for correct division by $(x + 1)$ or for the quadratic factor found by inspection, <u>and</u> the conclusion that no remainder means that $g(-1) = 0$  or inspection with at least two terms of three-term quadratic factor correct; or finding $f(6) = 0$  or $(x - 6)$ found as factor  for factors giving two terms of quadratic correct or for factors ft one error in quadratic formula or completing square; <b>M0</b> for formula etc without factors found  for those who have used the factor theorem to find $(x - 6)$ , <b>M1</b> for working with cubic to find that $(x + 1)$ is repeated  condone inclusion of ' $= 0$ '	NB examiners must use annotation in this part; a tick where each mark is earned is sufficient  M0 for trials of factors to give cubic unless correct answer found with clear correct working, in which case award the M1A1M1A1  allow for $(x - 6)$ and $(x + 1)$ given as factors eg after quadratic formula etc  isw roots found, even if stated as factors  just the answer $(x - 6)(x + 1)^2$ oe gets last 4 marks
			[2]		
			[5]		

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11	(i)	[radius =] $\sqrt{125}$ isw or $5\sqrt{5}$  [C =] (10, 2)	B1  B1  [2]	condone $x = 10, y = 2$	
11	(ii)	verifying / deriving that (21, 0) is one of the intersections with the axes  (-1, 0)  (0, -3) and (0, 7)	B1  B1  B2       [4]	using circle equation or Pythagoras; or putting $y = 0$ in circle equation and solving to get 21 and -1; condone omission of brackets  <b>B1</b> each;  if B0 for D and E, then <b>M1</b> for substitution of $x = 0$ into circle equation or use of Pythagoras showing $125 - 10^2$ or $h^2 + 10^2 = 125$ ft their centre and/or radius	equation may be expanded first  condone not written as coordinates  condone not written as coordinates; condone not identified as D and E; condone D = (0, 7), E = (0, -3) – will penalise themselves in (iii)

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11	(iii)	<p>midpt BE = <math>(21/2, 7/2)</math> oe</p> <p>grad BE = <math>\frac{7-0}{0-21}</math> oe isw</p> <p>grad perp bisector = 3 oe</p> <p><math>y - 7/2 = 3(x - 21/2)</math> oe</p> <p><math>y = 3x - 28</math> oe</p> <p>verifying that <math>(10, 2)</math> is on this line</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p><b>[6]</b></p>	<p>ft their E</p> <p>or stating that the perp bisector of a chord always passes through the centre of the circle</p> <p>ft their E;</p> <p>M0 for using grad BC (= <math>-2/11</math>)</p> <p>for use of <math>m_1m_2 = -1</math> oe soi; ft their grad BE;</p> <p>no ft from grad BC used</p> <p>ft; M0 for using grad BE or perp to BC</p> <p>allow this M1 for C used instead of midpoint</p> <p>must be a simplified equation</p> <p>no ft;</p> <p>A0 if C used to find equation of line, unless B1 earned for correct argument</p>	<p>NB examiners must use annotation in this part; a tick where each mark is earned is sufficient</p> <p>must be explicit generalised statement; need more than just that C is on this perp bisector</p> <p>condone <math>-1/3x</math> oe</p> <p>condone <math>3x</math> oe;</p> <p>allow M1 for eg <math>-1/3 \times 3 = -1</math></p> <p>or use of <math>y = 3x + c</math> and subst of <math>(21/2, 7/2)</math> oe ft</p> <p>no ft;</p> <p>those who assume that C is on the line and use it to find <math>y = 3x - 28</math> can earn B0M1M1M1A1A0</p> <p>those who argue that the perp bisector of a chord always passes through the centre of the circle and then uses C rather than midpt of BE are eligible for all 6 marks</p>



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12	(i)	$3x^2 + 12x + 13 = 2x + k$	M1	oe eg M1 for $3x^2 + 10x + 13 = k$	condone $3x^2 + 10x + 13 - k = y$ for this M1
		$3x^2 + 10x + 13 - k [= 0]$	M1	for rearranging to 0; condone one error in adding/subtracting; but M0 for $3x^2 + 10x + 13 = k$ or $3x^2 + 10x + 13 - k = y$	$3x^2 + 10x + 13 - k [= 0]$ will also earn the first M1 if a separate statement has not already done so
		$b^2 - 4ac > 0$ oe soi	M1	may be earned near end with correct inequality sign used there	allow ' $b^2 - 4ac$ is positive' oe; 0 for just 'discriminant $> 0$ ' unless implied by later work
		$100 - 4 \times 3 \times (13 - k) (> 0)$ oe	M1	for correct substitution ft into $b^2 - 4ac$ , dep on second M1 earned; brackets / signs must be correct	can be earned with equality or wrong inequality, or in formula
		$k > 14/3$ oe	A1	accept $k > 56/12$ or better, isw incorrect conversion of fraction but not wrong use of inequalities	M0 for trials of values of $k$ in $b^2 - 4ac$
			[5]		

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12	(ii)	$3(x+2)^2 + 1$ www as final answer  y-minimum = 1 [hence curve is above x-axis]	B4          B1          [5]	<b>B1</b> for $a = 3$ and <b>B1</b> for $b = 2$  and <b>B2</b> for $c = 1$ or <b>M1</b> for $13 - 3 \times$ their $b^2$ or for $13/3 -$ their $b^2$ or <b>B3</b> for $3 \left[ (x+2)^2 + \frac{1}{3} \right]$  Stating min pt is $(-2, 1)$ is sufft allow ft if their $c > 0$  B0 for only showing that discriminant is negative oe; need also to justify that it is all above not all below x-axis  B0 for stating min point = 1 or ft	condone omission of square symbol;  ignore equating to zero in working or answer          must be done in this part; ignore wrong x-coordinate
12	(iii)	5 cao	B2          [2]	<b>M1</b> for substitution of their $(-2, 1)$ in $y = 2x + k$	allow M1 ft their $3(x+2)^2 + 1$ ; or use of $(-2, 1)$ found using calculus; M0 if they use an incorrect minimum point inconsistent with their completed square form